

# The internal gravity wave spectrum: A new frontier in global ocean modeling

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- Others including many members of the NSF-funded Climate Process Team led by Jennifer MacKinnon of Scripps

# Motivation

- Breaking internal gravity waves drive most of the mixing in the subsurface ocean.
- The internal gravity wave spectrum is just starting to be resolved in global ocean models.
- Somewhat analogous to resolution of mesoscale eddies in basin- and global-scale models in 1990s and early 2000s.
- Builds on global internal tide modeling, which began with 2004 Arbic et al. and Simmons et al. papers utilizing Hallberg Isopycnal Model (HIM) run with tidal forcing only and employing a horizontally uniform stratification.

## Motivation continued...

- Here we utilize simulations of the HYbrid Coordinate Ocean Model (HYCOM) with both atmospheric and tidal forcing.
- Near-inertial waves and tides are put into a model with a realistically varying background stratification.
- Nonlinear interactions fill out the frequency-wavenumber spectrum.
- Note other groups are following suit with tide+circulation models (Harper Simmons, personal communication; Dimitris Menemenlis, personal communication; Müller et al. 2012).
- Talk focuses on the development of an internal gravity wave spectrum, after briefly discussing our other results.

# Implementation of tides in HYCOM

- Add astronomical tidal potential of largest semidiurnal and diurnal constituents (8 in run analyzed here, 5 in newest runs)
- Add self-attraction and loading term (scalar approximation in run analyzed here, altimeter model in newest runs)
- Apply parameterized topographic wave drag to tidal part of flow in bottom 500 meters

# HYCOM vs TPXO $M_2$ barotropic tides (Shriver et al. 2012)

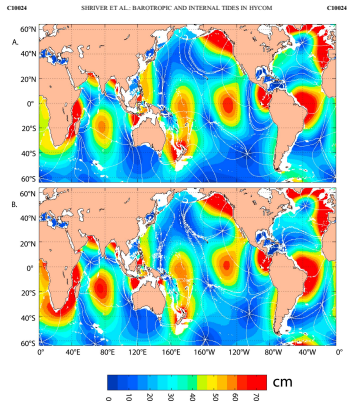


Figure 2. Amplitude (cm) of  $M_2$  surface tidal elevation in (a) TPXO 7.2 (an update to that described by Egbert et al. [1994]), a barotropic tide model constrained by satellite altimetry, and (b) HYCOM simulations in which the tide is unconstrained by satellite altimetry. Lines of constant phase plotted every  $45^\circ$  in Figures 2a and 2b are overlaid in white.

altimetry-constrained barotropic tide model [Egbert et al., 1994] and the internal tides in HYCOM is results from an analysis of along-track satellite altimetry data [Ray and Mitchum, 1996]. Several previous comparisons of modeled and observed internal tides have utilized regional models of strong internal tide generation sites forced by specified barotropic tides at their horizontal boundaries [e.g., Cummins et al., 2001; Kang et al., 2000; Merryfield et al., 2001].

# HYCOM vs along-track altimetric estimates of surface signature of $M_2$ internal tides (Shriver et al. 2012)

- Computed from high-passing total  $M_2$  signal

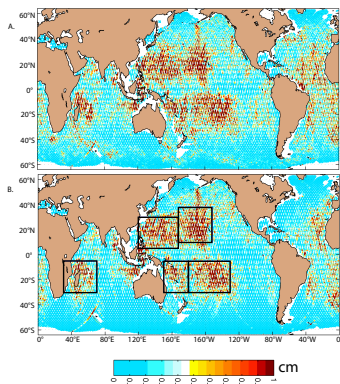


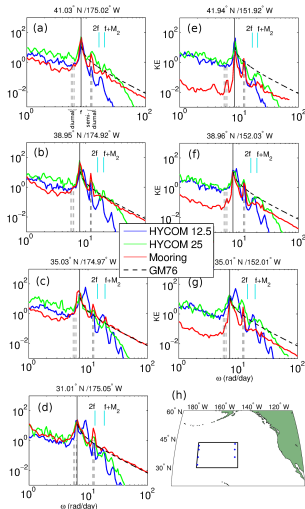
Figure 7. The  $M_2$  internal tide amplitude from the (a) altimetric-based and (b) HYCOM tidal analyses. The five subregions denoted by black boxes in (b) are used to compute the area-averaged amplitudes in Table 2.

# Now on to today's main topic...internal gravity wave spectrum

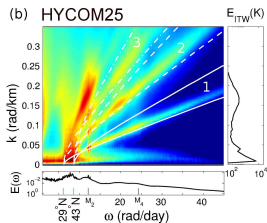
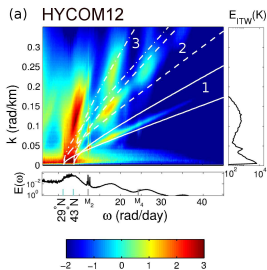


# Internal gravity wave kinetic energy frequency spectra (Müller et al. in press GRL)

- Note logarithmic smoothing employed.

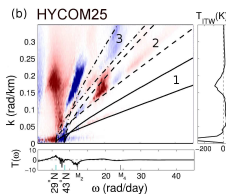
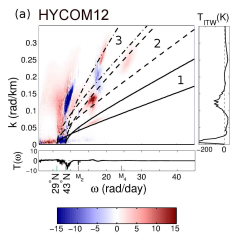


# Internal gravity wave kinetic energy frequency-horizontal wavenumber spectra (Müller et al. in press GRL)



# Nonlinear internal gravity wave kinetic energy frequency-horizontal wavenumber spectral transfers (Müller et al. in press GRL)

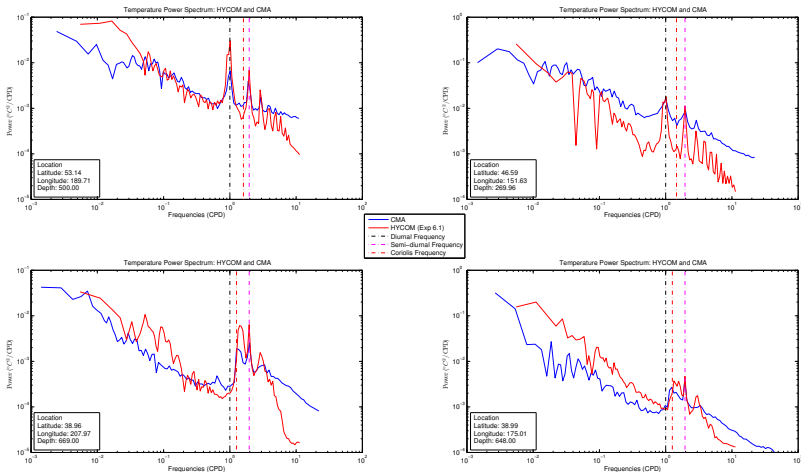
- $T(k, \omega) = \text{Re}[-\widehat{\vec{u}}^* \cdot \widehat{[\vec{u} \cdot \nabla \vec{u}]}]$



# Application of frequency-horizontal wavenumber spectrum to altimetry

- We will compute the frequency-horizontal wavenumber spectrum of SSH to separate low-frequency, internal tide, and non-tidal internal wave contributions.

# Frequency spectra of temperature (Bassette et al. and Luecke et al. in preparation)



# Summary

- Models with concurrent atmospheric and tidal forcing are beginning to develop an internal gravity wave spectrum, especially as resolution increases.
- Frequency-horizontal wavenumber spectrum of modeled internal gravity wave kinetic energy fills in along predicted linear dispersion curves, and fills out more completely with higher model resolution.
- Kinetic energy frequency spectra lie closer to observations, and nonlinear interactions are more vigorous, when model resolution is increased.
- We are now investigating internal gravity wave temperature variance.