

# Use of isopycnic-coordinate ocean models in long-term global simulations

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*Subtitle, slightly more to the point:*

Relaxing the incompressibility  
assumption in the isopycnic-  
coordinate ocean model HYCOM

# The issue

In HYCOM we traditionally

- (1) replace in-situ density  $\rho$  by potential density  $\rho_{pot}$
- (2) treat the fluid as **incompressible**.

According to Spiegel and Veronis (1960), these are defensible and mutually consistent approximations.

They create problems with thermobaricity.

More importantly, globally referenced  $\rho_{pot}$  is not necessarily monotonic in  $z$  in the real ocean.

What Spiegel and Veronis (1960) say:

The equations governing convection in a perfect gas are formally equivalent to those for an **incompressible** fluid if the static temperature gradient is replaced by its **excess over the adiabatic** ... and the following approximations are valid: (a) the vertical dimension of the fluid is much less than any scale height, and (b) the motion-induced fluctuations in density and pressure do not exceed ... the total static variations of these quantities.

## The issue (cont'd)

The Spiegel-Veronis approximation, combined with the use of  $\rho_{pot}$  as vertical coordinate, allows us to reduce the 2-term pressure gradient formula

$$\alpha \nabla_z p = \alpha \nabla p + g \nabla z$$

to a numerically stable 1-term expression:

$$\alpha \nabla p + g \nabla z = \nabla_{\alpha} (\alpha p + gz)$$

where  $\alpha$  now stands for the inverse of *potential* density  $\rho_{pot}$

# The finite-volume approach

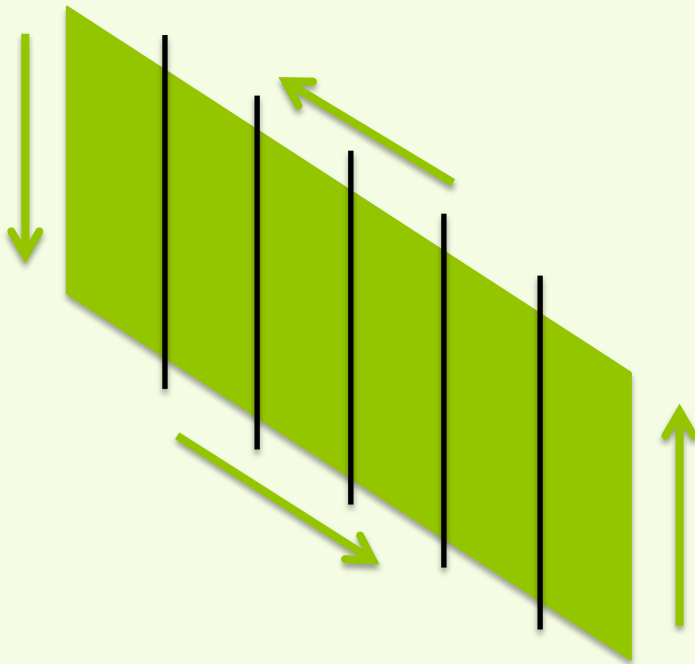
- Goal: use realistic eqn. of state to overcome limitations of the Spiegel-Veronis approach. This requires reverting to the numerically problematic 2-term pressure gradient formula.
- The approach of Adcroft et al<sup>(1)</sup> is to replace the 2-term finite-difference PGF expression by a line integral of “contact pressure” along the perimeter of each grid cell in the vertical.

(1) Adcroft, A., Hallberg, R. and M. Harrison, 2008: A finite volume discretization of the pressure gradient force using analytic integration. *Ocean Modelling*. 22, (3-4), 106-113.

# Green's Theorem:

$$\frac{1}{\text{cell area}} \iint_{\text{area}} \frac{\partial p}{\partial x} dx dz = \frac{1}{\text{cell area}} \oint_{\text{perimeter}} p \vec{k} \cdot d\vec{s}$$

“contact” pressure



Key to success:  
high accuracy on  
vertical segments  
of line integral

Fear of coding errors....



# Validating PGF code: test 1

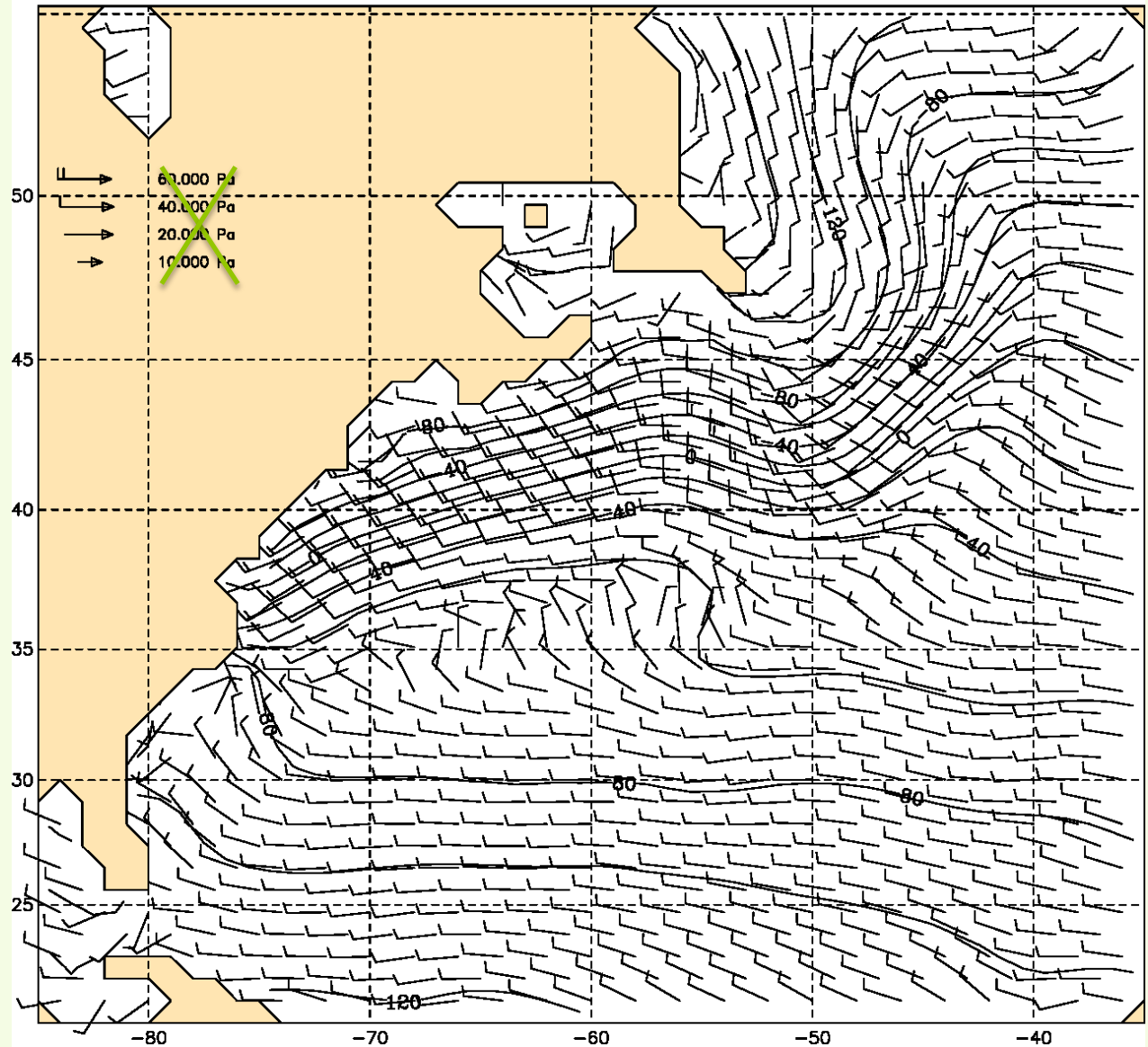
- Define spatially varying, strongly **sloping** layer interfaces and **rugged** bottom topography.
- Make  $T, S$  globally constant.
- Set sea surface height = 0.
- Get consistent bottom values of  $p$  and  $z$  via downward integration of hydrostatic eq<sup>n</sup>.
- Integrate upward to find  $gz$  where needed.
- Compute  $PGF$  at all grid points.
- Correct answer to look for:  $PGF = 0$  everywhere.

# Validating PGF code: test 2

- Use realistic model state, including spatially varying layer interfaces and bottom topography.
- Cook up variable  $SSH$  (for example, let  $SSH \sim SST$ ).
- Set  $T, S = const$  in **uppermost** model layer.
- Get consistent bottom values of  $p$  and  $z$  via downward integration of hydrostatic eq<sup>n</sup>.
- Integrate upward to find  $gz$  where needed.
- Overlay top-layer geostrophic velocity vectors on  $SSH$  map.
- Check whether velocity vectors **exactly** follow  $SSH$  contours.

layer 1 velocity yr 0.00 (dec.31) hyclv12h

Testing the PGF code  
in Hycom: surface  
**geostrophic** flow  
superimposed on sea  
surface height



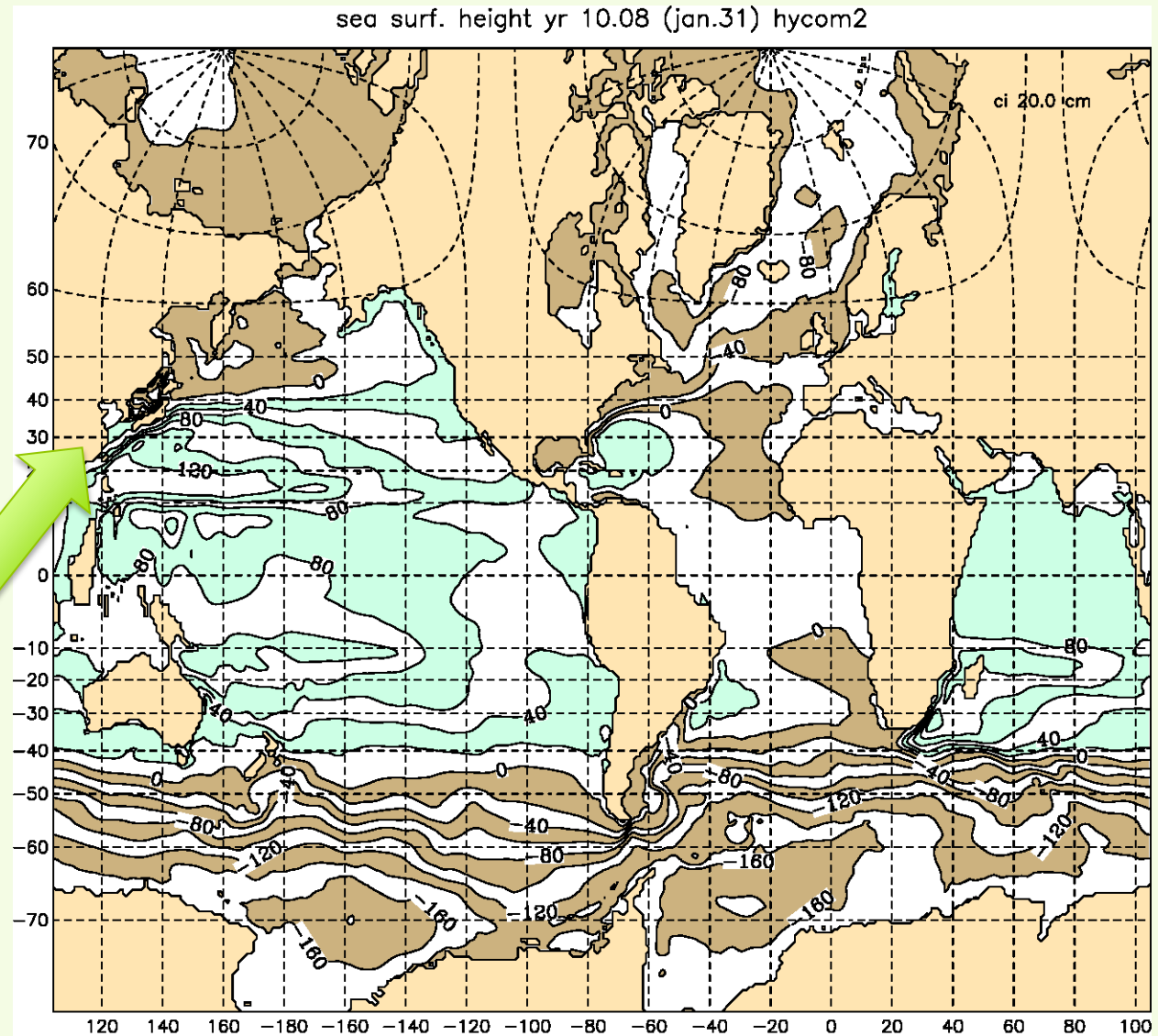
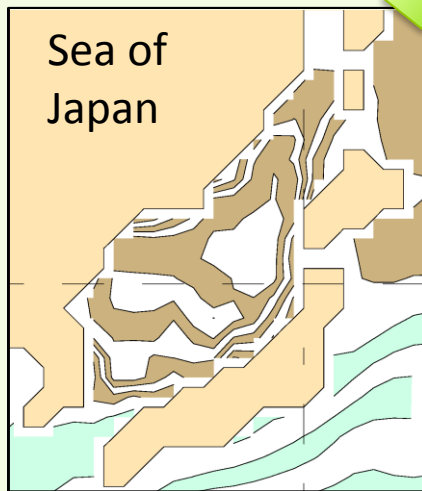
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# HycomC

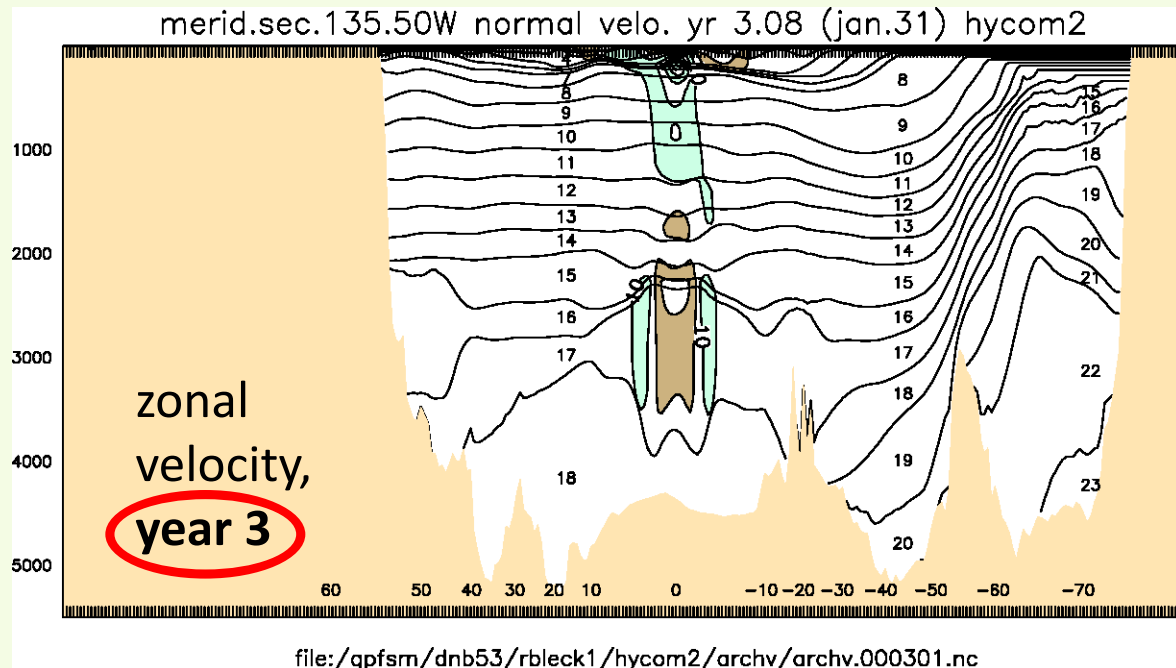
(=*hycom* using  
*compressible*  
*eqn. of state*)

Monthly-averaged  
sea surface height,  
January **year 10**

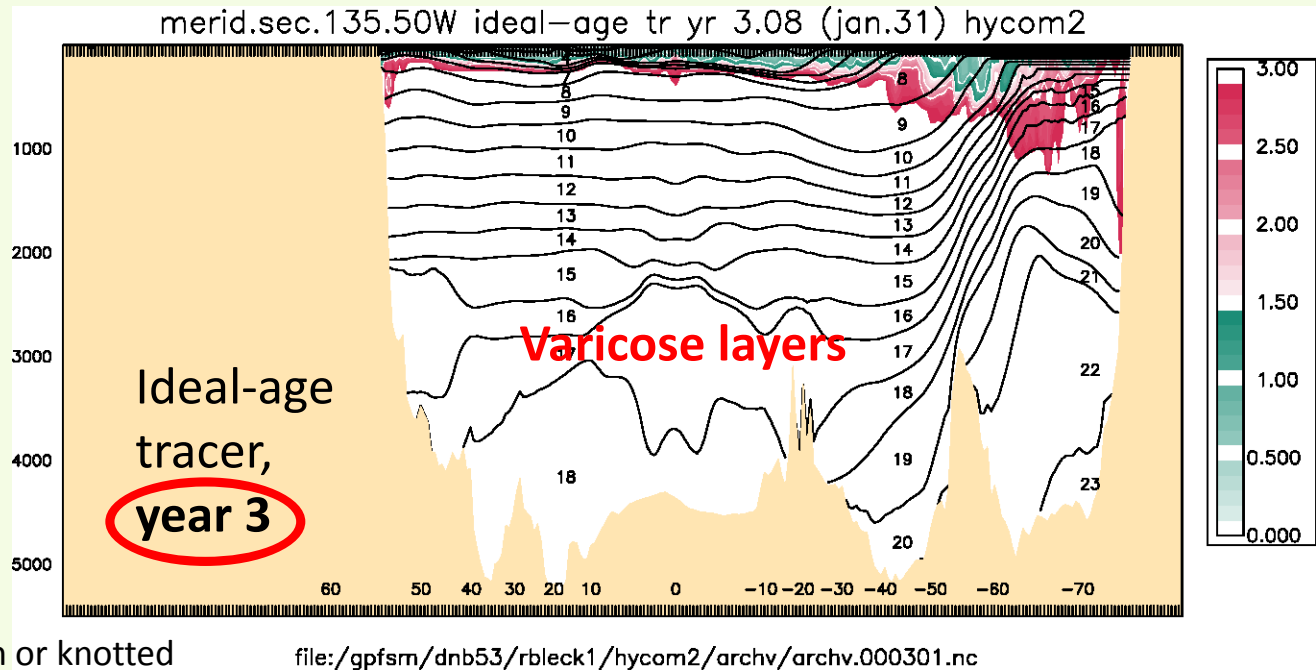


# HycomC

(=hycom using compressible eqn. of state)



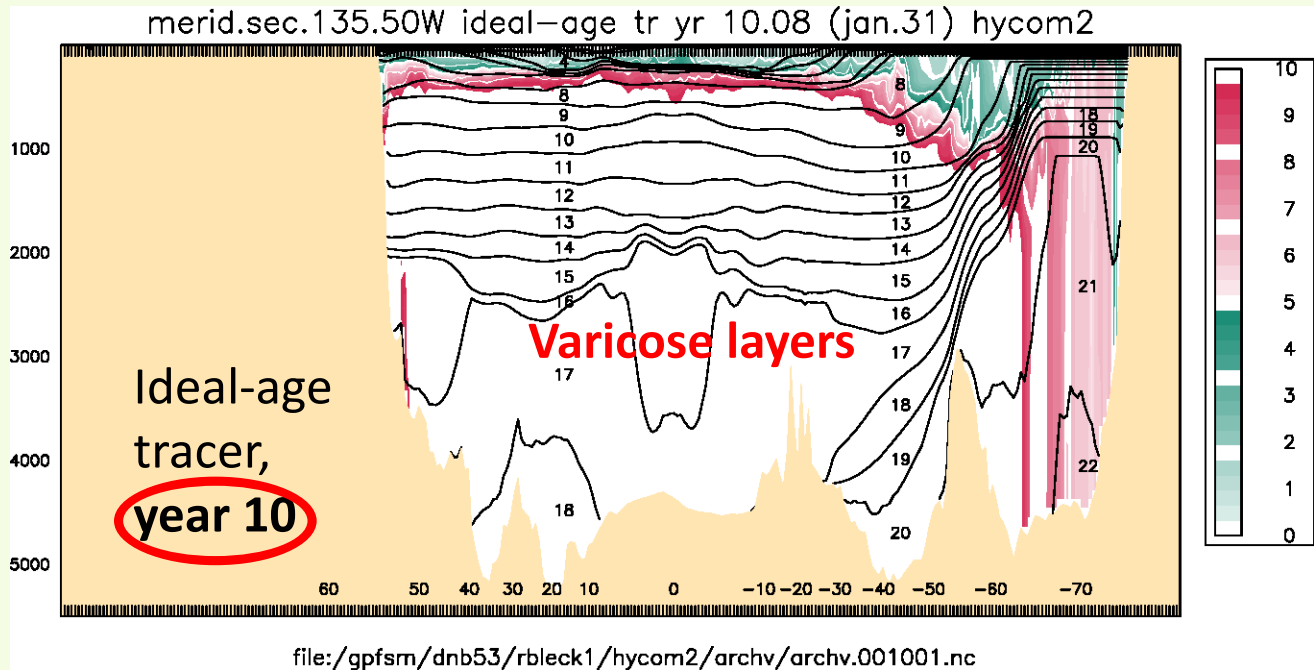
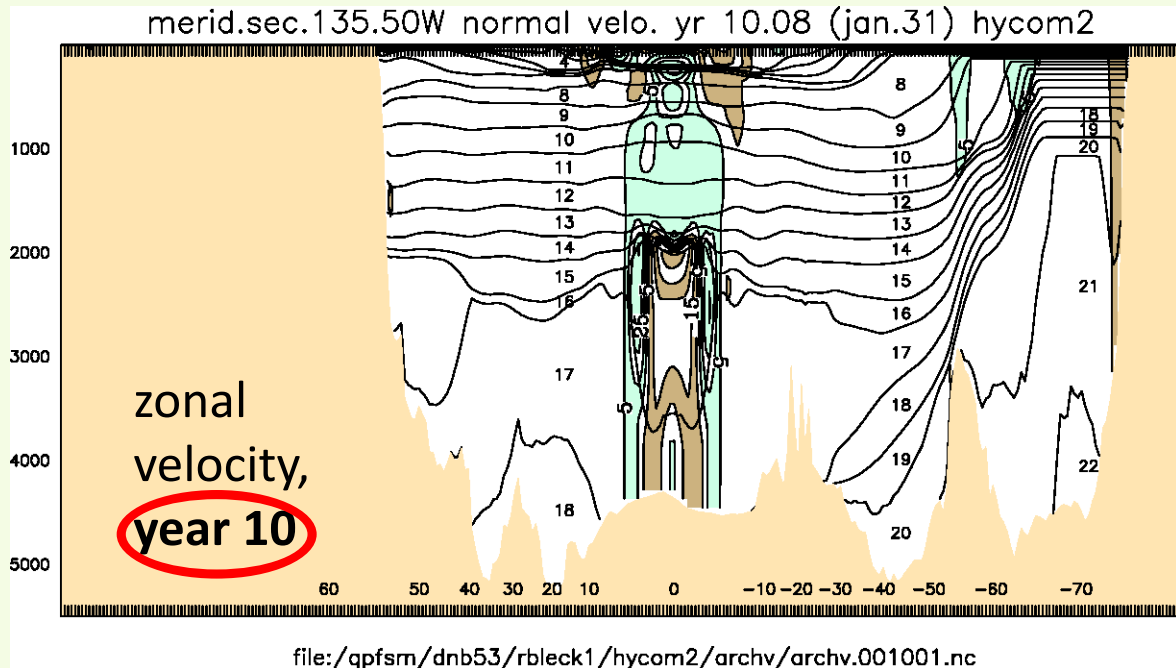
Cross sections show additional problems ... mid-depth varicose<sup>1</sup> layers



<sup>1</sup>varicose = abnormally swollen or knotted

# HycomC

(=hycom using compressible eqn. of state)



What might create the varicose layers .... the grid generator?



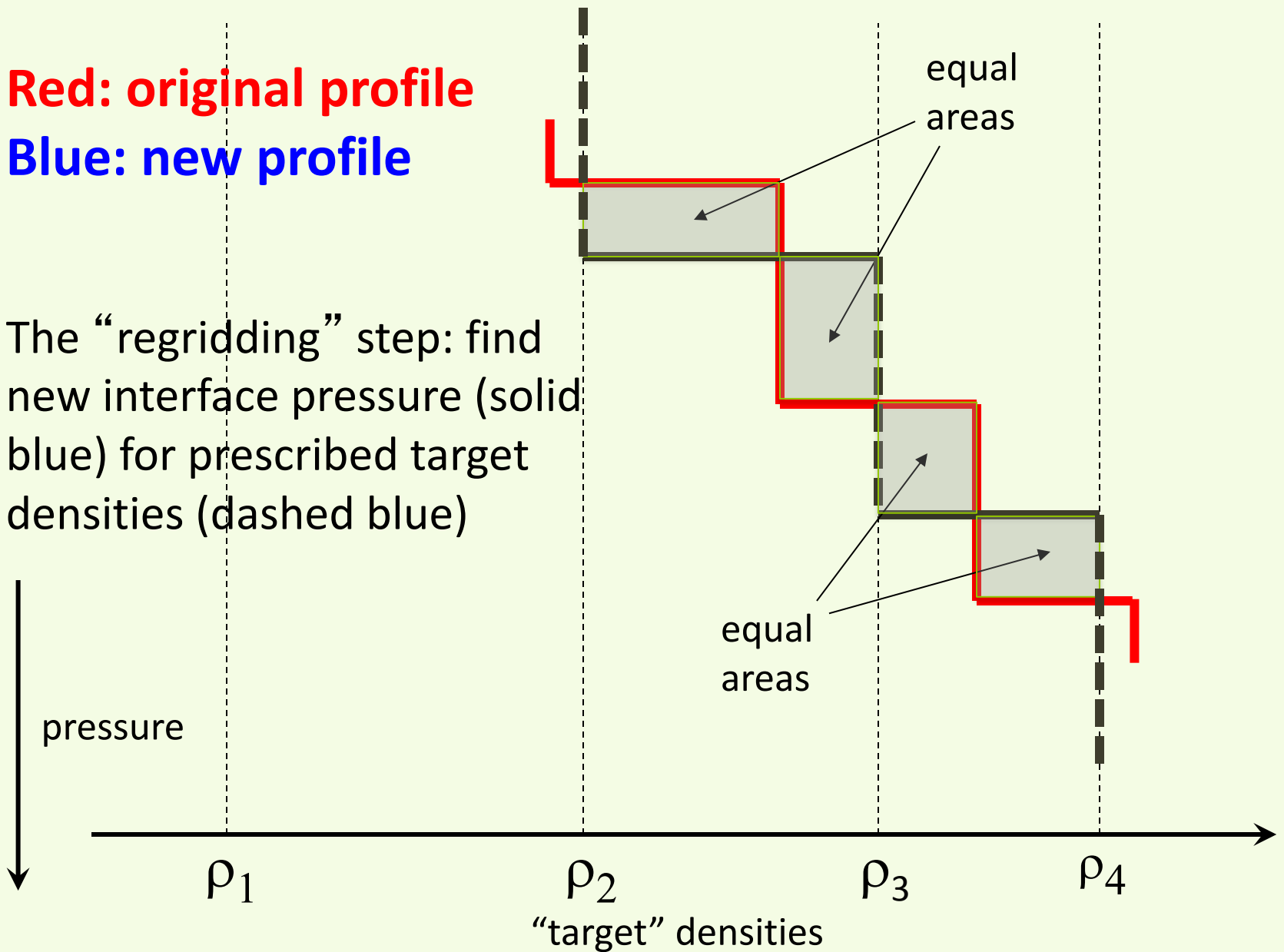
# How the vertical grid generator works

- Step 1: transform input staircase density profile to isopycnic coordinates (i.e. **regrid** vertical profile so as to restore layer densities to target).
- Step 2: Inflate massless layers created in step 1, starting at the top and stopping at the first layer not requiring inflation.
- Step 3 (common to all grid generators): **remap** vertical T/S profiles.



**Red: original profile**  
**Blue: new profile**

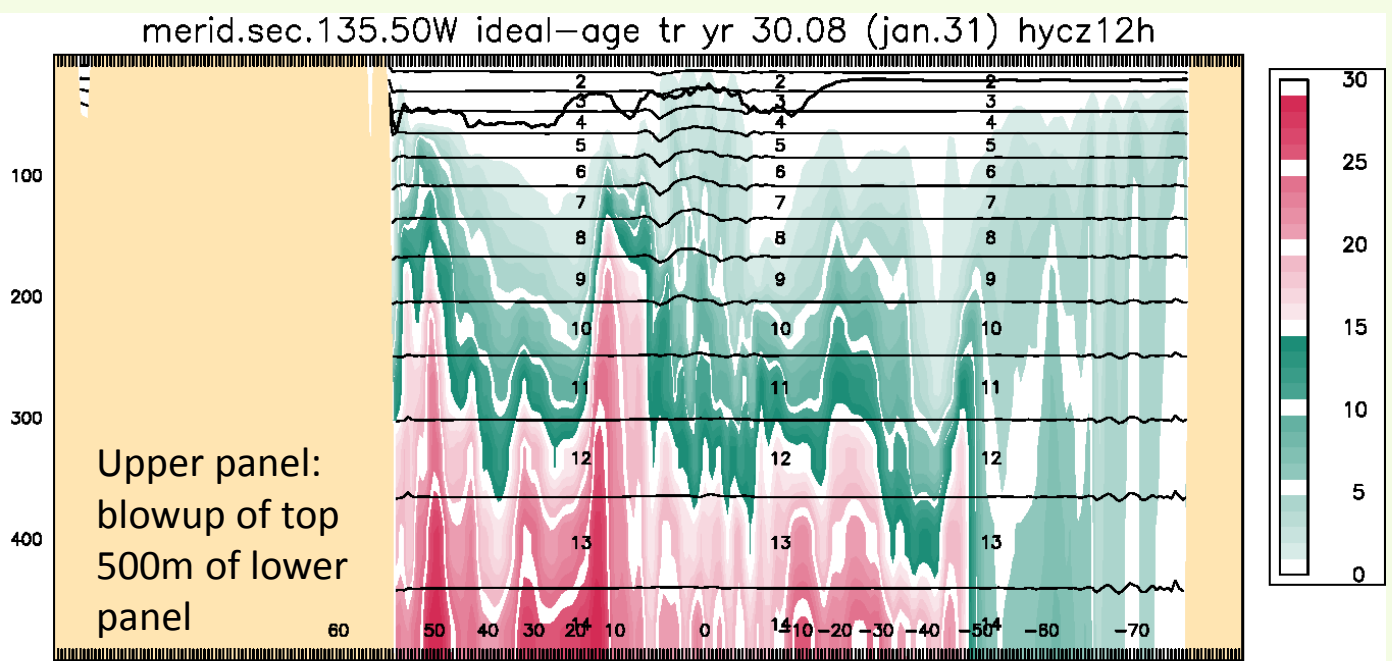
The “regridding” step: find new interface pressure (solid blue) for prescribed target densities (dashed blue)



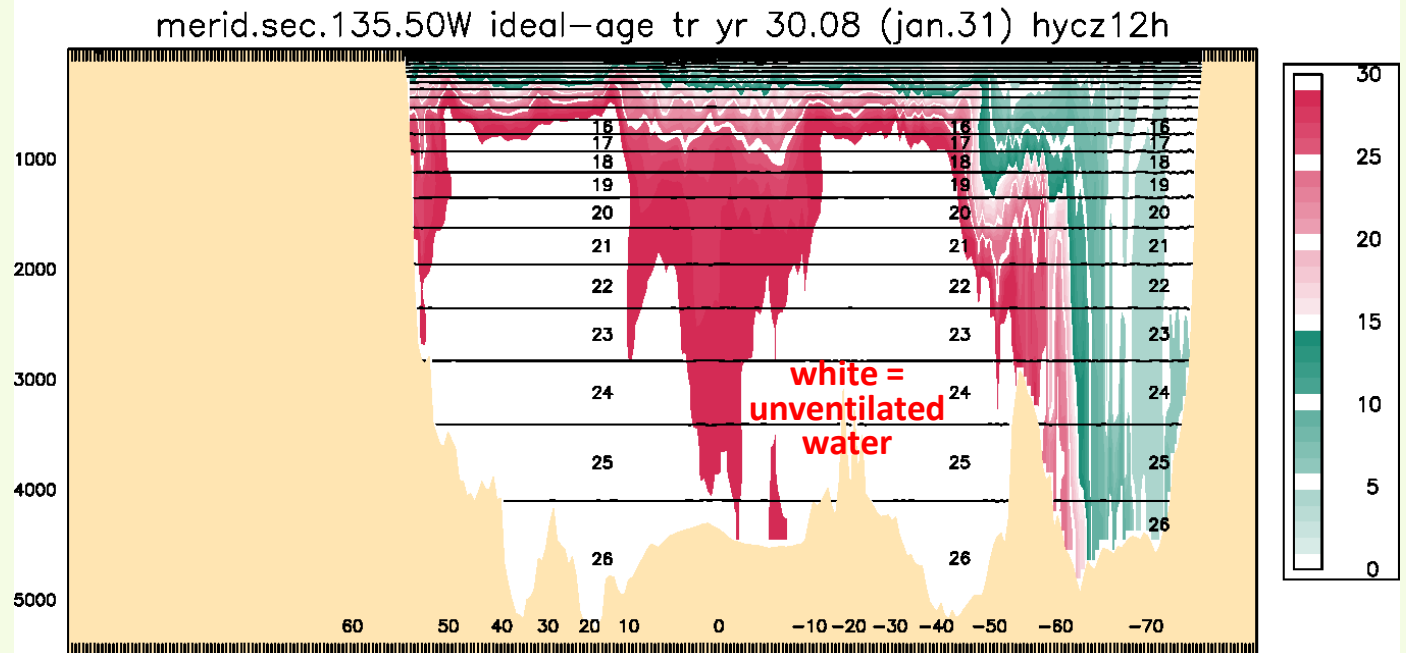
# Are grid generator problems surmountable?

- Fallback option: give up on restoring toward **isopycnic** layer structure.
- Instead, restore toward **level** surfaces. **Heresy**
- Make restoration slow enough to render layers **quasi-material** during passage of gravity waves.
- Retain HYCOM's adaptive-coordinate features
  - continue to allow massless layers on sea floor (e.g. “shrink wrap” seamounts, etc);
  - unrestricted choice of bottom depth levels unrelated to interface depths.

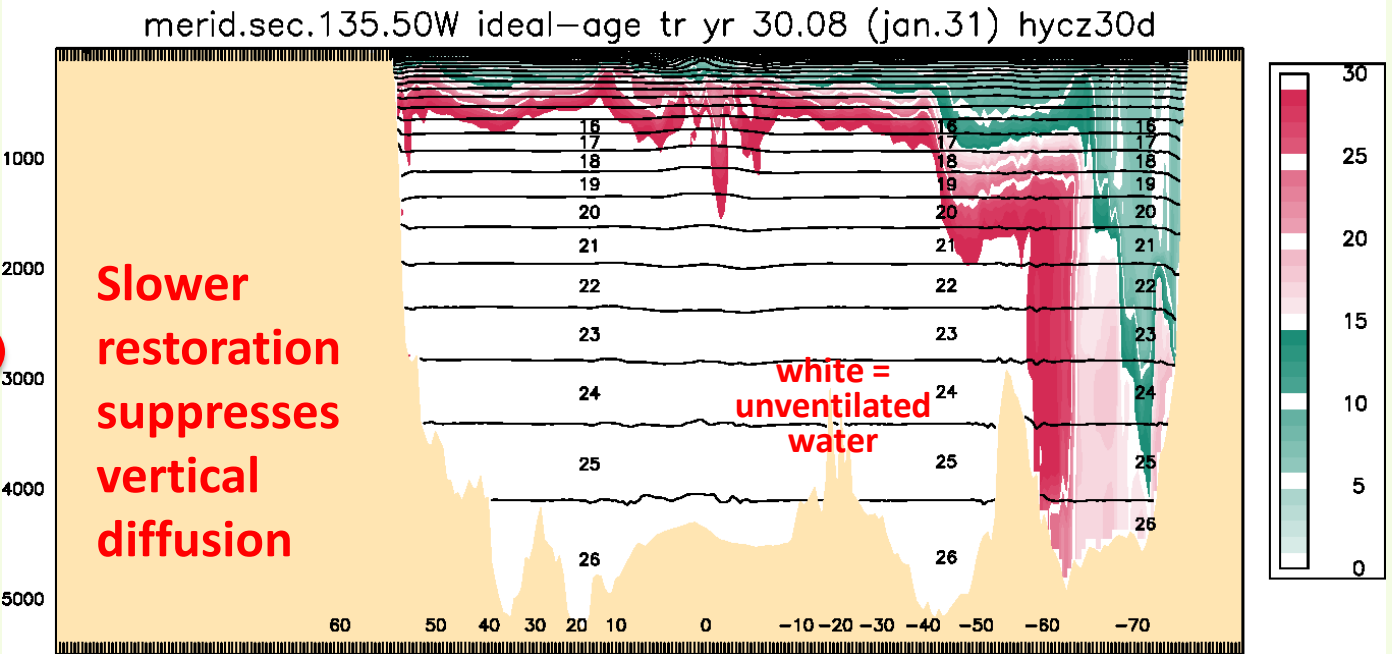
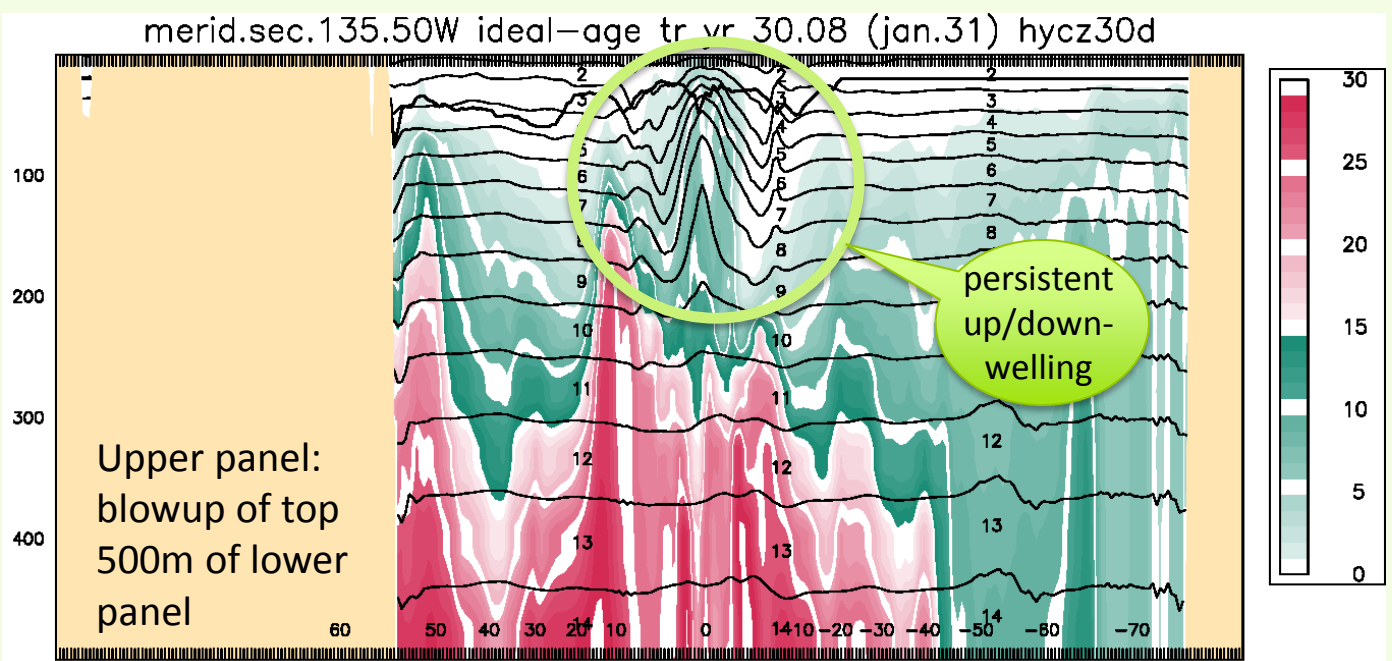
**HycomZ**  
(=hycom with compressible eqn. of state and restoration toward **level** surfaces)



Ideal-age tracer  
at yr 30, **12-hr**  
coordinate  
restoring time



**HycomZ**  
 (=hycom with compressible eqn. of state and restoration toward **level** surfaces)



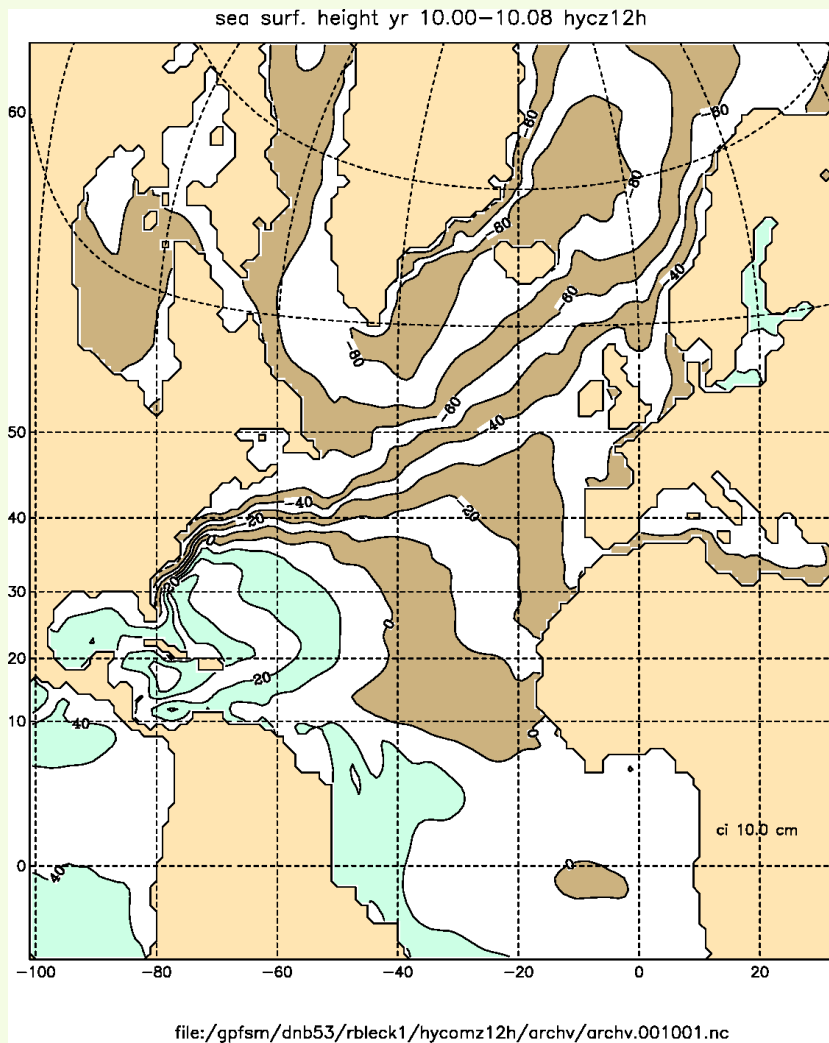
# Preliminary Findings (as of April 2015)

- The finite-volume PGF approach seems workable in HYCOM, paving the way for eventual removal of the traditional Boussinesq-related dual approximation of (1) treating ocean water as incompressible and (2) using potential density as buoyancy-controlling variable (*Spiegel and Veronis, 1960*).
- Long-term degeneracies in the isopycnic layer field presumably are caused by deficiencies in the present vertical grid generator.
- Simulations based on initialization with (and relaxation toward) level coordinate surfaces are successful.
- With sufficiently long relaxation times, HycomZ (the new compressible isobaric-layer version of HYCOM) retains its material-coordinate character with respect to passing gravity waves.

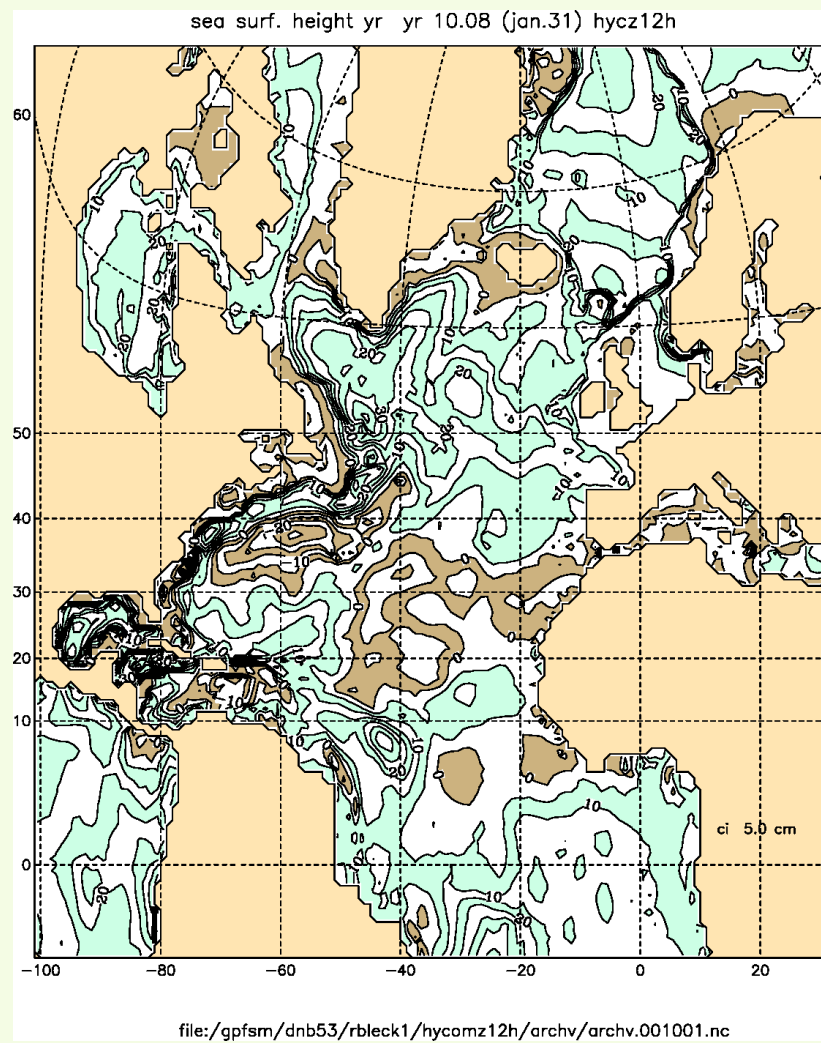
This is work in progress.

A recent letdown (as of June  
2015)...

## Sea-surface height, **monthly** average



## Sea-surface height, snapshot



HycomZ simulation, 12-hr interface restoring time

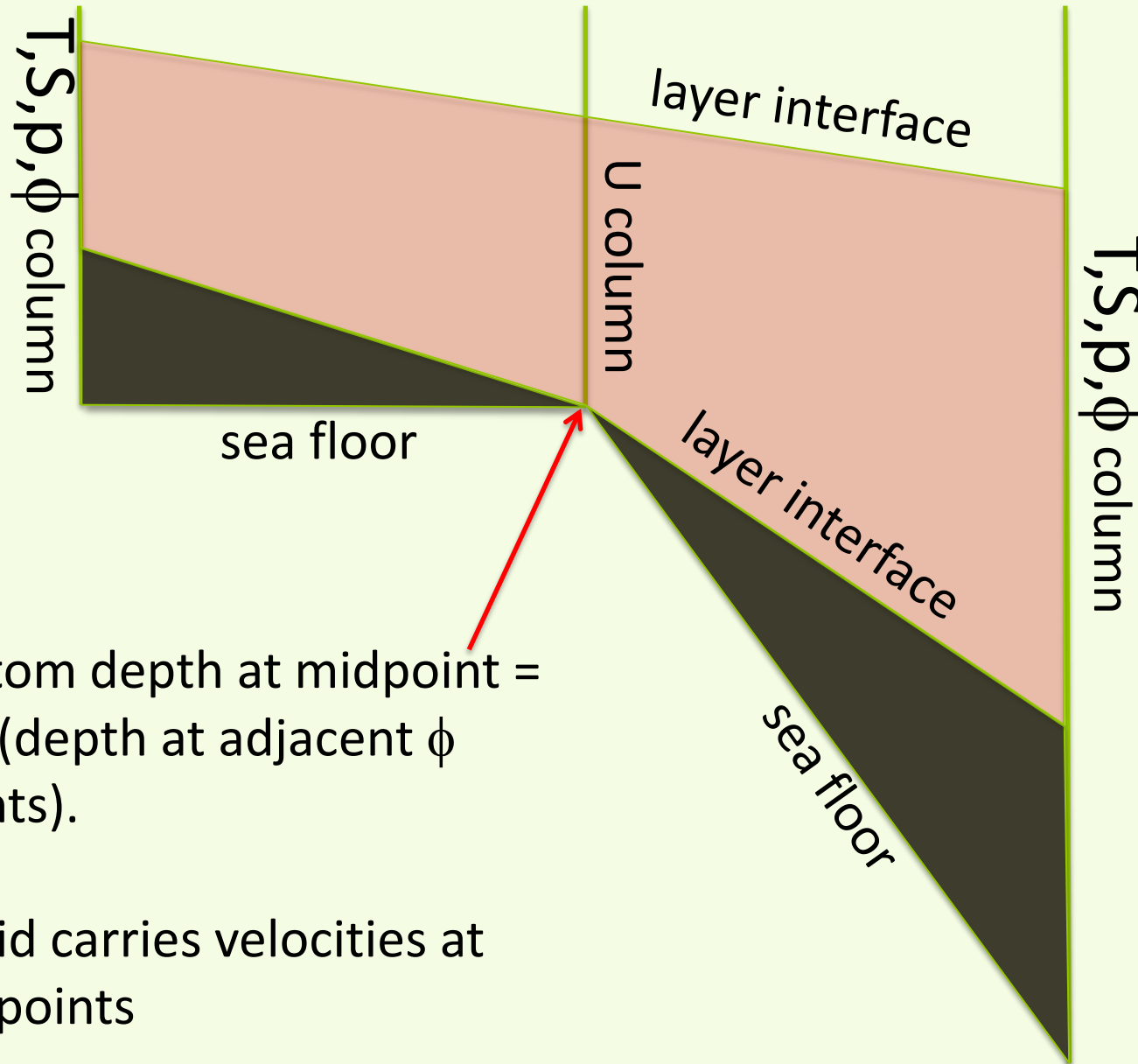
On this somewhat pessimistic note ...

Thank you



Unused slides follow

# Finite-volume approach: treatment of bottom cells



Bottom depth at midpoint =  $\min(\text{depth at adjacent } \phi \text{ points})$ .

C grid carries velocities at midpoints

How generalized-vertical coordinate models typically compute horizontal pressure gradients:

