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4	Impact of horizontal resolution (1/12° to 1/50°) on Gulf		
5	Stream separation, penetration, and variability		
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8	Eric P. Chassignet		
9	Xiaobiao Xu		
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11	Center for Ocean-Atmospheric Prediction Studies (COAPS)		
12	Florida State University		
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23	Corresponding author: echassignet@fsu.edu		
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#### Abstract

The impact of horizontal resolution (1/12° to 1/50°; 6 to 1.5 km at mid-latitudes) on Gulf 26 27 Stream separation, penetration, and variability is quantified in a series of identical North Atlantic 28 experiments. The questions we seek to address are two-fold: (a) Is the realism of the modeled 29 solution increased as resolution is increased? and (b) How robust is the modeled mesoscale and 30 sub-mesoscale eddy activity as a function of grid spacing and how representative is it of interior quasigeostrophic (QG) or surface quasigeostrophic (SQG) turbulence? We show that (a) the 31 32 representation of Gulf Stream penetration and associated recirculating gyres shifts from unrealistic 33 to realistic when the resolution is increased to 1/50° and when the non-linear effects of the 34 submesoscale eddies intensifies the mid-latitude jet and increases its penetration eastward, (b) the penetration of into the deep ocean drastically increases with resolution and closely resembles the 35 36 observations, and (c) surface power spectra in the 70-250 km mesoscale range are independent of 37 the horizontal resolution and of the latitude, and are representative of 2D QG and SQG turbulence. 38

#### 1. Introduction

39 Convergence studies are unusual because parameters are often changed as resolution is 40 increased. Here, we follow in the footsteps of Hurlburt and Hogan (2000), Smith et al. (2000), 41 Oschlies (2002), Bryan et al. (2007), Levy et al. (2010), Thoppil et al. (2011), Marzocchi et al. 42 (2015), and Biri et al. (2016) by reporting on the impact of horizontal resolution  $(1/12^{\circ} \text{ to } 1/50^{\circ})$ 43 on Gulf Stream separation, penetration, and variability using a series of identical North Atlantic 44 experiments. The questions we seek to address are two-fold: (a) Is the realism of the modeled 45 solution increased as resolution is increased? and (b) How robust is the modeled mesoscale and sub-mesoscale eddy activity as a function of grid spacing and how representative is it of interior 46 47 quasigeostrophic (QG) or surface quasigeostrophic (SQG) turbulence?

48 It is generally recognized that a minimum resolution of  $1/10^{\circ}$  is required for a proper 49 representation of mid-latitudes western boundary currents and associated eddies (Paiva et al., 50 1999; Smith et al., 2000; Maltrud and McClean, 2005; Chassignet and Marshall, 2008). A grid 51 spacing of 1/10°, however, is not sufficient to resolve the Rossby radius of deformation with two 52 grid points at all latitudes (Hallberg, 2013) and therefore does not allow for a proper representation 53 of baroclinic instability and associated eddies throughout the domain. Furthermore, effective 54 resolution is limited by the numerical dissipation range (Soufflet et al., 2016) and models with 55 resolution on the order of 1/10° are now being referred as eddying models while eddy-resolving 56 models are configurations that truly resolve the first Rossby radius of deformation throughout the 57 domain (CLIVAR Exchanges special issue, 2014). Despite the major improvements observed with 58 1/10° grid spacing, the solutions remain extremely sensitive to choices in boundary conditions and 59 subgridscale parameterizations (Ezer and Mellor, 2000; Chassignet and Garraffo, 2001; Bryan et 60 al., 2007; Chassignet and Marshall, 2008) and there is a continuous need to quantify the value

61 added of increased resolution. Furthermore, horizontal resolution of the O(1) km is required to explicitly resolve submesoscale motions with an horizontal scale of the O(10) km. Submesoscale 62 physics have been shown to play a significant role in the vertical fluxes of mass, buoyancy, and 63 64 tracers (Thomas et al., 2008; Capet et al., 2008; Fox-Kemper et al., 2008; Klein et al., 2011; Roullet 65 et al., 2012; Capet et al., 2016). However, only a few studies have been able to report on the impact 66 of the submesoscale motions on the large scale oceanic circulation because of the computing cost 67 associated with numerical simulations with O(1) km grid spacing. Using a hydrodynamic (no 68 active thermodynamics) model, Hurlburt and Hogan (2000) showed a significant improvement in 69 western boundary current pathways with increased resolution  $(1/16^\circ, 1/32^\circ, \text{ and } 1/64^\circ,$ 70 respectively). Levy et al. (2010) compared the mean characteristics of an idealized flat bottom 71 basin-scale seasonally subtropical and subpolar gyres configuration in a suite of numerical 72 experiments varying in horizontal resolution  $(1^\circ, 1/9^\circ, \text{ and } 1/54^\circ)$ . They found that the non-linear 73 effects of the submesoscale eddies that emerge at  $1/54^{\circ}$  strongly intensifies the jet that separates 74 the two gyres, making it more zonal and penetrating further to the east. The authors states that their 75 results are presumably highly constrained by the idealized geometry of their domain, but we find 76 that many of their results carry over to our series of identical North Atlantic experiments  $(1/12^\circ,$ 77  $1/25^{\circ}$ , and  $1/50^{\circ}$ , respectively).

In this paper, we show that (a) the representation of Gulf Stream penetration and associated recirculating gyres shifts from unrealistic to realistic when the resolution is increased to 1/50°, (b) the penetration of EKE into the deep ocean is drastically different and closely resembles observations, and (c) surface power spectra in the 70-250 km mesoscale range are independent of the horizontal resolution and of the latitude, and are representative of 2D QG and SQG turbulence (k<sup>-5</sup> SSH spectra in energetic regions, not as steep in quiescent regions). The paper is organized as

84 follows. Section 2 describes the model configuration and spin-up procedure. The surface mean and 85 turbulent circulation is discussed in section 3 as a function of resolution and in comparison to observations. It also focuses on the impact of ageostrophic motions on the representation of surface 86 87 eddy kinetic energy and the fact that current altimetry measurements likely underestimates surface 88 eddy kinetic energy by as much as 30%. The impact of resolution on the deep ocean circulation is 89 shown to be quite significant in section 4. Power spectra are used in section 5 to quantify the degree 90 of 2D QG and SQG turbulence present in the numerical simulations. Finally, the results are 91 summarized in section 6.

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# 2. Model configuration and spin-up

93 The HYbrid Coordinate Ocean Model (HYCOM) configuration used in this paper is identical 94 to that of Xu et al. (2010, 2012, 2014, 2015, 2016) and covers the North Atlantic from 28°S to 95 80°N (Fig. 1). The vertical coordinate in HYCOM (Bleck, 2002) is isopycnal in the stratified open 96 ocean and makes a dynamically smooth and time dependent transition to terrain-following in 97 shallow coastal regions and to fixed pressure levels in the surface mixed layer and/or unstratified seas (Chassignet et al., 2003; Chassignet et al., 2006). No inflow or outflow is prescribed at the 98 99 northern and southern boundaries. Within a buffer zone of about 3° from the northern and southern 100 boundaries, the 3-D model temperature, salinity, and depth of isopycnal interface are restored to 101 the monthly Generalized Digital Environmental Model (GDEM) (Teague et al., 1990; Carnes, 102 2009) climatology with an e-folding time of 5-60 days that increases with distance from the 103 boundary.

The horizontal resolution for the three experiments are  $1/12^{\circ}$ ,  $1/25^{\circ}$ , and  $1/50^{\circ}$  (9, 4.5, and 2.25 km at the equator; 6, 3, 1.5 km in the Gulf Stream region, respectively). The  $1/12^{\circ}$  model topography is based on the 2' Naval Research Laboratory (NRL) digital bathymetry database,

107 which combines the global topography based on satellite altimetry of Smith and Sandwell (1997) 108 with high-resolution regional databases several ("http: 109 //www7320.nrlssc.navy.mil/DBDB2\_WWW" for documentation). The 1/25° and  $1/50^{\circ}$ 110 topographies are linearly interpolated from the  $1/12^{\circ}$  topography and do not contain additional 111 high-resolution topographic features. In the vertical, the simulation contains 32 hybrid layers with 112 density referenced to 2000 m ( $\sigma_2$ ): 28.10, 28.90, 29.70, 30.50, 30.95, 31.50, 32.05, 32.60, 33.15, 113 33.70, 34.25, 34.75, 35.15, 35.50, 35.80, 36.04, 36.20, 36.38, 36.52, 36.62, 36.70, 36.77, 36.83, 36.89, 36.97, 37.02, 37.06, 37.09, 37.11, 37.13, 37.15, and 37.20 kg m<sup>-3</sup>. The 1/12° configuration 114 resolves the first Rossby radius of deformation up to 60°N while the 1/50° resolves it everywhere 115 116 (Hallberg, 2013). Furthermore, the 1.5 km grid spacing of the  $1/50^{\circ}$  configuration resolves up to 117 the fifth internal Rossby radii of deformation at mid-latitudes, based on the above density 118 distribution of the hybrid layers. As in Chassignet and Garraffo (2001) and Xu et al. (2010), the horizontal viscosity operator is a combination of Laplacian (A<sub>2</sub> = max( $0.05\Delta x^2$  x deformation 119 tensor, A) and bihamonic (A<sub>4</sub> = V<sub>4</sub> $\Delta x^3$ ). The viscosity and diffusion parameters are listed in Table 120 1. The values for the coefficients in the  $1/25^{\circ}$  decrease as a function of the grid size and are half 121 122 that of the  $1/12^{\circ}$ . The values for the coefficients in the  $1/50^{\circ}$  are kept close to that of the  $1/25^{\circ}$ , in 123 order to isolate the impact of resolving the submesoscale on the solution. The K-profile 124 parameterization of Large et al. (1994) is used for vertical mixing in the surface mixed layer as well as in the ocean interior. The bottom drag is quadratic with a coefficient of  $10^{-3}$  and a 125 background RMS flow speed of  $5 \times 10^{-2}$  m/s. 126

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Sea-ice related processes are modeled using an "energy loan" where freezing takes place whenever latent heat is needed to keep the mixed layer temperature from dropping below the freezing level. When the ocean-ice system is being heated, the incoming energy is used to melt the ice before the water temperature is allowed to rise above the freezing level (Semtner, 1976).

134 The three configurations are initialized using potential temperature and salinity from the 135 GDEM climatology and were spun-up from rest for 20 years (Fig. 2) using climatological 136 atmospheric forcing from the ECMWF reanalysis ERA40 (Uppala et al., 2005) with 3-hourly wind 137 anomalies from the Fleet Numerical Meteorology and Oceanography Center 3 hourly Navy 138 Operational Global Atmospheric Prediction System (NOGAPS) for the year 2003. The year 2003 139 is considered to be a neutral year over the 1993-present time frame in term of long-term 140 atmospheric pattern the North Atlantic Oscillation (NAO). Heat fluxes are computed using the 141 bulk formulae of Kara et al. (2005). The freshwater flux (evaporation, precipitation, and river 142 runoffs) is treated as a virtual salinity flux and the sea surface salinity (SSS) is restored to monthly 143 climatology with a piston velocity of 15 m/30 days. The salinity difference (between model and 144 climatology) in SSS restoring is clipped to be 0.5 psu to diminish the damping effect of the 145 restoring on ocean fronts (see Griffies et al, 2009, for a discussion). There is no tidal forcing.

Figure 2 shows the time evolution of the mean kinetic energy for the three experiments. It takes approximately 5 years for the energy to stabilize which is the time it takes for the first baroclinic mode Rossby wave to cross the Atlantic basin. The 1/25° is 50% more energetic than the 1/12°, not surprising since the viscosity/dissipation was cut in half when the resolution was increased. The 1/50°, on the other hand, has a mean kinetic energy level similar to the 1/25°. This is expected since the viscosity/dissipation was kept close to that of the 1/25° as the resolution was increased. The slight increase in mean kinetic energy is attributed to the increase in mesoscale and submesoscale activity (discussion in section 3.b). Other integrated values such as the Florida
Straits transport (30.8, 34.8, and 34.9 Sv, respectively) and the average overturning streamfunction
at 26°N (17.7, 17.8, and 17.5 Sv respectively) are in reasonable agreement with the observed
values of ~32 Sv (e.g., Meinen et al., 2010) and ~17Sv (e.g., McCarthy et al., 2015), respectively.

157 **3.** Surface fields

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#### a. Mean circulation

159 The mean SSH and the mean surface kinetic energy over the last 5 years of the three 160 simulations are compared to the mean SSH field derived from observations (Rio et al., 2014) over 161 the Gulf Stream region (30-80°W, 30-55°N) in Figs. 3 and 4, respectively. Traditionally, a proper 162 representation of the Gulf Stream separation in ocean numerical models has been a challenge (see 163 Chassignet and Marshall, 2008, for a review) and still remains an issue for many configurations 164 despite the fact the major improvements are realized when one uses an horizontal resolution on 165 the order of  $1/10^{\circ}$  (Bryan et al., 2007). In all three simulations, the Gulf Stream separates at the 166 correct location at Cape Hatteras, but its eastward penetration into the interior differs greatly. At 167 1/12°, the modeled Gulf Stream (Fig. 3e) does not penetrate far into the interior and the 168 recirculating gyre (Fig. 3e) and highest eddy kinetic energy (Figs. 7c, 8c) are confined west of the 169 New England seamounts (60°W), results that have already been reported in Chassignet and 170 Garraffo (2001), Haza et al. (2007), and Chassignet and Marshall (2008). The 1/25° simulation 171 does not show a lot of improvement over the 1/12° simulation. It is arguably worse since the Gulf 172 Stream in the 1/25° simulation not only does not extend as a coherent feature past the New England 173 seamounts (Fig. 4d), it exhibits an unrealistically strong recirculating gyre southeast of Cape 174 Hatteras (Fig. 3d), and has excessive surface variability (Figs. 7d, 8d) west of 60°W. It is only 175 when the resolution is increased to  $1/50^{\circ}$  (Fig. 3c) that the Gulf Stream system appears to settle in

a pattern that resembles the observations (Fig. 3a). The Gulf Stream penetration, recirculation gyre,
and extension qualitatively compare very well with the latest AVISO CNES-CLS mean dynamic
topography (MDT) (Fig. 3a).

179 In order to validate the position of the current main axis as well as the width and intensity of 180 the currents, one needs to be able to perform quantitative model-data comparisons on the scales of 181 interest (i.e., tens of kilometers). There is not of lot of in-situ observations that can be directly 182 compared to the model results on those scales, but global climatologies have come a long way by 183 combining altimetry, direct measurements, and surface drifters (see Rio et al., 2014 for a review) 184 and are now able to provide MDT fields with a sharp definition of the western boundary ocean 185 currents and associated fronts. There is however still quite a few uncertainties associated with these 186 climatologies as shown by the differences between the 2009 and the 2013 CNES-CLS  $1/4^{\circ}$ 187 climatologies (Fig. 3a,b) (Rio et al., 2011, 2014, respectively). Improvements in the 2013 MDT 188 from the 2009 MDT arise mostly from using a geoid based on the GOCE (Gravity and Ocean 189 Circulation Experiment) instead of one based on the previous Gravity Recovery and Climate 190 Experiment (GRACE) mission and from removing previously undetected undrogued drifters from 191 the drifting buoy velocities distributed by the Surface Drifter Data Assembly Center (SD-DAC) 192 (Grodsky et al., 2011).

193 Comparison of the model results to these climatologies can be supplemented by comparison to 194 mean dynamic topography constructed along altimetric satellite ground tracks using direct in-situ 195 measurements (Carnes et al., 1990; Blaha and Lunde, 1992; Chassignet and Marshall, 2008). Fig. 196 5a shows the location of bathythermographic data taken during flights under the TOPEX altimeter 197 ground track 93253A in September 1993 (courtesy of the Altimetry Data Fusion Center, Naval 198 Oceanographic Office) where the mean dynamic topography was computed making the

199 assumption that the dynamic topography relative to the geoid can be approximated by the dynamic 200 height relative to a deep pressure surface which is parallel to the geoid (i.e., a level of no motion). 201 Any error in this assumption will lead to different values of mean dynamic topography, but for the 202 spatial scales of interest, as long as the level of no motion is deep enough, choosing a different 203 level just adds or removes a bias. Fig 5b shows the mean SSH along track 93253A from 204 observations (derived from the bathythermographic data, CNES-CLS09, and CNES-CLS13) and 205 from the 3 numerical simulations  $(1/12^\circ, 1/25^\circ)$ , and  $1/50^\circ)$ . The latest CNES-CLS13 climatology 206 is closest to the MDT derived from the bathythermographic data while the CNES-CLS09 profile 207 shows a much stronger southern recirculation, very likely from contamination by the undrogued 208 drifters which are significantly impacted by wind slippage (Rio et al., 2014). As expected, the 209  $1/50^{\circ}$  simulation is closest to the observations with an SSH slope very close to the observations. 210 The slope is weaker in both the  $1/12^{\circ}$  and  $1/25^{\circ}$  simulations with the  $1/25^{\circ}$  exhibiting the biggest 211 departure south of 36°N where the model is unrealistically energetic.

212 The 5-year modeled mean surface velocity can also be compared to the long term 20-year 213 ADCP mean velocity measurements (Fig. 6) made by the Oleander between the U.S. East Coast 214 and Bermuda (Rossby et al., 2014) from 1993 to 2012. As for the mean SSH, the mean position 215 and direction of the  $1/50^{\circ}$  current vectors is closest to the observations with the  $1/25^{\circ}$  being too far 216 south and oriented meridionally and the  $1/12^{\circ}$  being too zonal. The width of the Gulf Stream is 217 however slightly wider in the  $1/50^{\circ}$  model than in the observations, indicating more fluctuations 218 of the mean axis of the Gulf Stream in the model. The maximum mean speed of the  $1/50^{\circ}$  modeled 219 Gulf Stream (0.9 m/s) is also a little less than observed (~1 m/s) (Rossby et al., 2010, 2014).

b. <u>Fluctuations</u>

221 Figure 7 shows the root mean square (RMS) of the SSH for the AVISO observations and the 222 three numerical simulations. The AVISO observations are based on 20 years of altimetry (1993-223 2012) and the modeled RMS fields are for the last 5 years of the simulations. As mentioned above 224 in section 3a, both the  $1/12^{\circ}$  and  $1/25^{\circ}$  eddy variability are confined west of 60°W and the chain 225 of New England seamounts. The 1/25° simulation also shows excessive variability southwest of 226 the Gulf Stream axis, which is reflected in the mean SSH field. The overall distribution of the RMS 227 SSH in the  $1/50^{\circ}$  is in reasonable agreement with the observations, especially the zonal extent, but 228 it is significantly larger in magnitude, especially around the New England seamounts. We will 229 argue below that the difference is primarily due to the fact that altimetry only resolves eddies on 230 O(150) km over a 10-day window. The RMS SSH results reported here are consistent with the 231 distribution obtained by Hurlburt and Hogan (2000) using the 6-layer hydrodynamic (no active 232 thermodynamics) NLOM model (Fig. 8). They also found that the eddy variability remained west 233 of the New England seamounts for their  $1/16^{\circ}$  and  $1/32^{\circ}$  (equivalent to our  $1/12^{\circ}$  and  $1/25^{\circ}$ ) and 234 extend south for their  $1/32^{\circ}$ . It is only at  $1/64^{\circ}$  (equivalent to our  $1/50^{\circ}$ ) that the variability extends 235 further eastward. This seems to imply that resolving submesoscale features of the O(10) km is a 236 prerequisite for a correct eastward penetration of the Gulf Stream and the establishment of the 237 recirculating gyres.

Figure 9 displays the observed and modeled surface EKE generated using the geostrophic velocities computed from the SSH fields. As for the RMS, the overall distribution of the surface 1/50° EKE is in reasonable agreement with the observations, especially the zonal extent, but it is significantly larger in magnitude. The surface EKE shown in Fig. 9, however, does not take into account ageostrophic motions and this raises the question as to how significant is the ageostrophic EKE component. Presumably, ageostrophic flows should become more significant as the 244 resolution is increased and submesoscale features arise. Fig. 10 displays the difference between 245 the two components. The most striking feature is the asymmetry between the areas north and south 246 of the Gulf Stream main axis, with the ageostrophic contribution being negative (positive) south 247 (north) of the Gulf Stream. This asymmetry can be explained by considering that the largest 248 ageostrophic contribution arises in area where the flow curvature is significant (meanders, eddies) 249 and where the velocities deviate from geostrophy and satisfy the gradient wind balance, i.e., a 250 primary balance between the centripetal acceleration, the Coriolis acceleration, and the horizontal 251 pressure gradient force (Douglass and Richman, 2015). Outside the Gulf Stream and high energetic 252 areas, the surface Ekman flow becomes dominant. Ageostrophic motions are approximately 10 to 253 20% of the total velocity in energetic areas of the Gulf Stream and can be as high as 200% in areas 254 dominated by the surface Ekman flow (Fig. 11). A zoom on the region defined by the red rectangle 255 in Figure 11 shows that the ageostrophic motion in the eddies is always anticyclonic (Fig. 12). 256 This is because the centrifugal force associated with the flow curvature is not taken into account 257 when using the geostrophic balance, which results in the rotational velocities being under (over) 258 estimated in anticyclones (cyclones) (Chassignet et al., 1990).

259 The EKE map displayed in Figure 9a was derived from along track measurements optimally interpolated on a regular 1/4° grid by AVISO. By construction, the optimal interpolation filters 260 261 many of the scales present in nature and is therefore not 100% representative of the observations 262 on space scales less than 150 km (due do measurement noise and errors) and time scales less than 263 10 days (repeat cycle of the altimeters). In order to investigate the impact of the sub sampling and 264 optimal interpolation on the EKE fields, the 1/50° model outputs were filtered to be more 265 representative of the AVISO gridded outputs. To quantify the impact of the filtering, we compute 266 the SSH wavenumber power spectrum in the  $1/50^{\circ}$  configuration over the  $10^{\circ}$  by  $20^{\circ}$  box shown

in Figure 11. Over this energetic area, the  $1/50^{\circ}$  modeled power spectrum slope is  $k^{-5}$  in the 70-267 268 250 km mesoscale band (red in Fig. 13) and is representative of QG turbulence (see section 5 for 269 a complete description of the power spectra distribution over the domain). Figure 13 illustrates the 270 impact of the filtering on the wavenumber power spectrum. First, the subsampling of the model 271 outputs to the  $1/4^{\circ}$  grid removes any information below 35 km (green in Fig.13). Time averaging 272 the outputs over 10 days (dark blue in Fig. 13) or applying a 150 km band pass filter (turquoise in 273 Fig.13) bring the power spectrum slope closer to AVISO (black in Fig. 13), but it is only when the 274 two are applied together (purple in Fig. 13) that the modeled wavenumber spectrum resembles 275 most closely that of AVISO. This result is consistent with Biri et al. (2016) who report that the 276 spectrum derived from a 10 day resampled 4 km model follows more closely the altimeter 277 spectrum due to aliasing (see also Arbic et al. (2013), who performed a similar exercise, but for 278 spectral fluxes instead of spectra). Applying both the 10- day and 150 km band pass filters to the 279 model outputs leads to EKE plots (Fig. 14) that resembles more closely the AVISO-derived EKE 280 suggesting that the AVISO-derived EKE underestimates the observed EKE by approximately 30% 281 in the Gulf Stream region. One should note, however, that even filtered, the modeled surface EKE 282 is higher than observed south of the New England seamounts, suggesting that interactions with the 283 topography may be overemphasized in the model.

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# 4. Interior flows

Most model-data comparisons usually focus on the surface fields because of the scarcity of long time series at depth covering a large spatial area. Scott et al. (2010), expending on the work of Penduff et al. (2006) and Arbic et al. (2009), used a large collection of moored current meter records to assess the ability of three eddying global ocean models (POP, OCCAM, and HYCOM with 1/10° to 1/12° grid spacing), which resolve the first Rossby radius of deformation throughout

290 most of the domain (i.e. up to 55-60°N), to simulate the time-averaged total kinetic energy 291 throughout the water column. They found that the models agreed within a factor of two above 292 3500 m, and within a factor of three below 3500 m. Penduff et al. (2006) suggested that horizontal 293 resolution was probably the most important factor limiting their 1/6° global model in generating 294 realistic eddy kinetic energy, but Scott et al. (2010)'s results were not conclusive in that respect. 295 Thoppil et al. (2011) did however find that increasing the model resolution to  $1/25^{\circ}$  significantly 296 increased the surface and the abyssal EKE and clearly demonstrated that a better representation of 297 upper ocean EKE is a prerequisite for strong eddy-driven abyssal circulation. In this section, we 298 do show that horizontal resolution has a large impact on the distribution of interior kinetic energy by comparing the three simulations to eddy kinetic energy maps generated from moorings and 299 300 floats.

301 In Figures 15 and 16, vertical sections of modeled zonal velocities and eddy kinetic energy 302 along 55°W are compared to sections based on long term observations using drifters, floats, and 303 moored current meters (Richardson, 1985). 55°W is perhaps one of the most observed section 304 across the Gulf Stream with measurements first during POLYMODE (Richardson, 1985) and then 305 during SYNOP (Bower and Hogg, 1996). In this region, most of the deep oceanic variability is 306 generated by the surface currents via vortex stretching. It is very weak at  $1/12^{\circ}$ , in agreement with 307 the Scott et al. (2010) results. But it does increases significantly at the model resolution is refined 308 and, at  $1/50^{\circ}$ , the level and the pattern of the vertical zonal velocities and eddy kinetic energy 309 resemble most closely the observations. This is consistent with Thoppil et al. (2011)'s statement 310 that the surface and abyssal ocean circulation are strongly coupled through the energy cascades 311 that vertically redistribute the energy and vorticity throughout the entire water column.

312 There are not that many spatial distributions of EKE at depths from observations. The few that 313 exists are based on float measurements (SOFAR or Argo) and vary greatly in coverage and 314 sampling. Figure 17 compares the modeled EKE distribution at 700 m to EKE derived from several 315 years of SOFAR floats measurements (Richardson, 1993). As for the vertical sections, the 1/50° 316 EKE distribution is closest to the observations, with a 1000 cm<sup>2</sup>/s maximum west of the New 317 England seamounts and an 800 cm<sup>2</sup>/s extension past the seamounts. At 1000 m, the Argo floats 318 data used by Ollitrault and Colin de Verdière (2014) to derive the EKE do not provide the fine 319 temporal and spatial coverage of the SOFAR floats and the modeled 1/50° EKE differs 320 significantly (Fig. 18). Filtering the modeled outputs over a 30-day time window and 100 km as 321 for the Argo data leads to an EKE distribution that is much closer to the Ollitrault and Colin de Verdière (2014) map (Fig. 18a, c). As for the vertical sections, the magnitude of the  $1/12^{\circ}$  and 322 323 1/25° EKE distribution at 700 m and 1000 m are significantly less than in the 1/50° (Figs. 17,18).

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## 5. Wavenumber spectra distribution

325 Wavenumber spectra are a useful tool to quantify the energy and variability associated with 326 different scales and regions. In this section, we seek to address the questions of how robust is the 327 modeled mesoscale and submesoscale eddy activity as a function of grid spacing and how 328 representative is it of interior quasigeostrophic (QG) or surface quasigeostrophic (SQG) turbulence 329 (Le Traon et al., 2008). The wavenumber spectra distribution is computed over the North Atlantic 330 domain using boxes as in Le Traon et al. (1990), Paiva et al. (1999), Xu and Fu (2012), Richman 331 et al. (2012), Sasaki and Klein (2012), and Dufau et al. (2016) among others. There is some 332 sensitivity to the way spectra are computed and we follow Sasaki and Klein (2012) by making the 333 box doubly periodic in both the zonal and meridional directions following Lapeyre (2009). Cosine 334 tapered windows are also often used in the literature instead of the doubly periodic method (see

for example Richman et al. (2012) which use a 10% cosine taper window) and in order to document the impact of the method, we compare in Figure 19 the spectra computed using several cosine taper windows (none, 5%, 10%, 20%, and 40%) and the doubly periodic approach. For a cosine taper window greater than 10%, the results are very close to the doubly periodic (or mirror) approach. The latter method is therefore preferred for its simplicity and reproducibility. The model outputs used to compute the spectra are daily averages, except when discussing the impact of internal waves and inertial motions where hourly snapshots are used.

342 Figure 20 displays the one-year SSH wavenumber spectra over the Gulf Stream energetic 343 region  $(10^{\circ} \times 20^{\circ})$  box defined in Figure 11) computed from daily averaged outputs of year 20 for 344 the  $1/12^{\circ}$ ,  $1/25^{\circ}$ , and  $1/50^{\circ}$ , respectively. Over the mesoscale range of 70 to 250 km, the slope does 345 not vary as a function of the horizontal grid spacing and is  $k^{-5.1}$ ,  $k^{-4.9}$ , and  $k^{-5.0}$ , respectively. It is 346 now well documented that there is a strong seasonality associated with enhanced submesoscale 347 activity in the winter mixed layer (Mensa et al., 2013; Sasaki et al., 2014; Callies et al., 2015; 348 Rocha et al., 2016a). There is indeed a change in the slope of the SSH wavenumber spectra between 349 summer and winter at all resolution for scales less than 70 km, but it is more pronounced at  $1/12^{\circ}$ 350 than at  $1/50^{\circ}$  (Fig. 20). This does not mean that there is less small scales instabilities, just that the 351 SSH signature of the high Rossby number submesoscale features is less pronounced in this high 352 EKE region. The seasonality is clearly visible when comparing the relative vorticity distribution 353 between summer and winter in Figures 21 and 22 and when computing the energy and vorticity 354 spectra as in Figures 23 and 24. The difference in the number of small scale coherent features 355 between the  $1/12^{\circ}$  and the  $1/50^{\circ}$  is striking, both in the summer and the winter (Figs. 21 and 22). 356 But it is really at  $1/50^{\circ}$  that one can see an explosion of very small scale features during the winter 357 months (Fig. 22; see also Fig. 1 of Sasaki et al. (2014)).

358 Figures 23 and 24 compare the wavenumber spectra for SSH, energy, and relative vorticity 359 between two regions, the highly energetic Gulf Stream region (33°-43°N, 50°-70°W) as shown in 360 Figure 11 and a low EKE region (20°-30°N, 20°-40°W). In the 70-250 km mesoscale range, the SSH wavenumber spectra slope is  $k^{-4.2}$  in the low EKE region versus  $k^{-5}$  in the high EKE Gulf 361 362 Stream region. This is consistent with the results put forward by Richman et al. (2012) and Sasaki 363 and Klein (2012) which suggest that highly energetic regions are closer to QG turbulence and low 364 energetic regions closer to SQG turbulence. Further examination of the SSH, energy and relative 365 vorticity spectra (Figs. 21 and 22) in the two regions show additional differences. First, in the low 366 EKE region, the SSH wavenumber spectra slope exhibits a stronger seasonal cycle than in the high 367 EKE region which seems to indicate a stronger SSH signature of the smaller scale features in 368 winter. Second, the kinetic energy wavenumber spectra in the high EKE region does not differ 369 much when using either the total velocities or the geostrophic velocities. This is consistent with 370 the results of section 3b which showed that the ageostrophic component forms small percentage 371 of the total velocity. In the low EKE region, on the other hand, the wavenumber spectra slope in 372 the mesoscale range is reduced by 25% when using geostrophic velocities to compute the spectra. 373 Finally, the biggest difference is in the relative vorticity spectra which shows a stronger impact of 374 the seasonal cycle in the low EKE region in the 70-250 km mesoscale range.

The spatial distribution of the SSH wavenumber spectra from altimeter observations shows a large spatial latitudinal variability with slopes closer to -5 at mid-latitudes and as high as -1 in the tropics (Xu and Fu, 2011, 2012; Zhou et al., 2015; Dufau et al., 2016). As in previously published modeling results (Paiva et al., 1999; Richman et al., 2012, Biri et al., 2016), we do not find this latitudinal dependence in the 70-250 km band (Fig. 25): the slope is everywhere between -5 and -4. Several explanations have been put forward to explain the discrepancy including aliasing and 381 noise in the altimetry data (Biri et al., 2016), but it is also conceivable that one may underestimate 382 the impact of high frequency motions such as internal waves and tides when using daily averages 383 to compute the wavenumber spectra (Richman et al., 2012; Rocha et al., 2016b). In order to 384 investigate the impact of fast moving features, the wavenumber spectra of Figure 25 were re-385 computed using hourly snapshots (Fig. 26). The biggest difference between daily and hourly 386 spectra is in the tropics, mostly on scales below 70 km where the slopes can be as low as  $k^{-1}$ . The 387 impact of fast moving features on the 70-250 km wavenumber range is much smaller, i.e. a 388 decrease in the slope by up to 20% in a couple of 10° x 10° boxes (Fig. 26). Tides have been shown 389 to have a significant impact on the wavenumber spectra on small scales (see Fig. 9 of Rocha et al. 390 (2016b)), but does not appear to have an impact on the latitudinal dependence of the wavenumber 391 spectra in numerical models (Richman et al., 2012).

392

# 6. Summary and conclusions

393 In this paper, we quantify the impact of horizontal resolution  $(1/12^{\circ} \text{ to } 1/50^{\circ}; 6 \text{ to } 1.5 \text{ km at})$ 394 mid-latitudes) on a series of identical North Atlantic experiments. First, we find that the 395 representation of the Gulf Stream penetration and associated recirculating gyres shifts from 396 unrealistic to realistic when the resolution is increased to  $1/50^{\circ}$ . This is consistent with results 397 obtained by Hurlburt and Hogan (2000) using the 6-layer hydrodynamic NLOM model and by 398 Levy et al. (2010) using the NEMO model in an idealized domain. In all cases, the non-linear 399 effects of the submesoscale eddies that arise when the resolution reaches 1/50° intensifies the mid-400 latitude jet and increases its penetration eastward. Second, the penetration of the EKE into the deep 401 ocean drastically increases with resolution and closely resembles the observations in the 1/50° 402 configuration. And third, the wavenumber spectra are independent of horizontal resolution and 403 latitudes in the 70-250 km mesoscale range.

404 Convergence studies such as this one where most parameters are not changed, except for the 405 horizontal resolution, are unusual and the question arises as what one may expect as you continue 406 to increase the horizontal resolution, decrease viscosity, and/or increase the order of the numerical 407 schemes. At some point, for the right amount of internal dissipation and friction, the solution 408 should settle at a level close to the observations. In this paper, we showed that the level of EKE in 409 the  $1/50^{\circ}$  simulation was comparable to the observations when taking into account the aliasing 410 associated with the altimeter sampling, but with one caveat: it was obtained by prescribing absolute 411 winds at the ocean surface. While this is currently the norm for numerical models forced by an 412 atmospheric reanalysis product, this does not allow any ocean feedback to the atmosphere. This 413 feedback takes place via SST (see Small et al. (2008) for a review) and computation of the ocean 414 current/wind shear (see Renault et al. (2016a) for a review). Earlier studies have shown that the 415 latter can lead to a significant reduction of the surface EKE and Renault et al. (2016a) demonstrated 416 that, using a coupled model, the current feedback deflects energy from the geostrophic current into 417 the atmosphere and thus dampens eddies. Furthermore, the interaction of ocean eddies and the 418 atmosphere regulates western boundary currents (Ma et al., 2016). In particular, Renault et al. 419 (2016b) showed that the current feedback, through its "eddy killing" effect can stabilize the Gulf 420 Stream separation, a prerequisite for a proper separation and penetration (Özgökmen et al., 1997). 421 The reduction in surface EKE induced by the surface current feedback can be as high as 30%. This 422 means that future numerical simulations will need to be able to exhibit higher level of EKE when 423 using relative winds. As stated by Renault et al. (2016a), a bulk-forced oceanic uncoupled 424 simulation should prescribe the surface stress using the relative wind in a bulk formulae which 425 takes into account a parameterization of the partial re-energization of the ocean by the atmospheric 426 response. Renault et al. (2016a) propose a surface stress computed with the wind relative to the

427 current corrected by a current–wind coupling coefficient  $s_w$  as in  $U = U_a - (1-s_w)U_a$ . The value of 428 the coefficient  $s_w$  are estimated to be between .2 and .3 and can vary spatially (R. Abel, personal 429 communication).

430 In conclusion, it is fair to state that the next threshold for a significant improvement in western 431 boundary currents representation (i.e. Gulf Stream in this paper) is an increase in the horizontal 432 resolution from the eddying  $1/10^{\circ}$  to submesoscale enabled  $1/50^{\circ}$  grid spacing. Not only do the 433 results presented in this paper support some of the results put forward by Hurlburt and Hogan 434 (2000) and Levy et al. (2010), it also raises the question as the usefulness of intermediate 435 resolutions such as 1/25° or 1/36°, at least for the Gulf Stream region. The computational cost of 436 simulations at  $1/50^{\circ}$  is extremely large, and while currently available resources do not currently 437 allow for all the sensitivity experiments to numerical choices, stress formulations, vertical 438 resolution, tidal impact, etc., they will become more common in the future. Finally, we do realize 439 that this paper is somewhat descriptive, but it sets the stage for in-depth analyses of water mass transformations and associated transports that will be presented in a companion paper. 440

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	1/12°	1/25°	1/50°
Laplacian coefficient for momentum	20 m <sup>2</sup> /s	10 m <sup>2</sup> /s	10 m <sup>2</sup> /s
Biharmonic diffusive velocity (V4) for momentum	1 cm/s	1 cm/s	4 cm/s
Biharmonic diffusive velocity for layer thickness	1 cm/s	1 cm/s	4 cm/s
Laplacian diffusive velocity for tracers	0.5 cm/s	0.5 cm/s	1 cm/s

Table 1. Viscosity and diffusion coefficients

# **Figure Captions**

Figure 1. Model domain and bathymetry (in kilometers).

*Figure 2.* Time evolution of the domain-averaged kinetic energy (in  $cm^2s^{-2}$ ) for the three numerical experiments (1/12°, 1/25°, and 1/50°, respectively). The thin and thick lines denote monthly and annual averages, respectively.

*Figure 3. Time mean sea surface height (in cm) in the Gulf Stream region from a-b) the AVISO climatology CNES-CLS13 and CNES-CLS09, and c-e) the 1/50°, 1/25°, and 1/12° HYCOM simulations, respectively (years 16-20).* 

*Figure 4.* Kinetic energy (cm<sup>2</sup>s<sup>-2</sup>) of time mean surface geostrophic current based on a) the AVISO climatology CNES-CLS13, and b-d) the 1/50°, 1/25°, and 1/12°HYCOM simulations, respectively (years 16-20).

*Figure 5. a)* Topex-Poseidon tracks (#932523A in red) superimposed on the mean SSH (in cm) from Niiler et al. (2203), b) observed mean dynamic topography (in cm) along track #932523A derived from 1) the in-situ bathythermographic data, 2) the AVISO climatology CNES-CLS13 and CNES-CLS09, and 3) the 1/50°, 1/25°, and 1/12°HYCOM simulations, respectively (years 16-20).

*Figure 6.* a) Mean velocity section as measured by the Oleander (1993-2012) with shipboard ACDP (55 m depth). The horizontal bar corresponding to 1 m/s and 0.5 m/s for the variance ellipse (from Rossby et al., 2014); and b-d) mean velocity for the 1/50°, 1/25°, and 1/12° HYCOM simulations, respectively (years 16-20). The depth contours range from 1000 to 5000 meters (grey shading).

*Figure 7.* Sea surface height variability (in cm) in the Gulf Stream region, (a) based on AVISO (1993-2012) and (b-d) the 1/50°, 1/25°, and 1/12° HYCOM simulations, respectively (years 16-20).

*Figure 8.* Sea surface height variability (in cm) in the Gulf Stream region from three regional NLOM simulations at 1/16°, 1/32°, and 1/64° resolution (from Hurlburt and Hogan, 2000).

*Figure 9.* Eddy kinetic energy (EKE, in cm<sup>2</sup>s<sup>-2</sup>) in the Gulf Stream region computed from SSHderived geostrophic velocities: a) AVISO (1993-2012) and b-d) the 1/50°, 1/25°, and 1/12° HYCOM simulations, respectively (years 16-20).

*Figure 10.* Eddy kinetic energy (EKE, in  $cm^2s^{-2}$ ) difference between the EKE of the total current and the EKE of the geostrophic current. The negative contribution implies that the ageostrophic current is in opposite direction to the geostrophic current.

*Figure 11. Ratio of ageostrophic current speed to the total current speed for the month of February of model year 20. The red 20°x10° box denotes the area shown in Figure 12.* 

*Figure 12.* Averaged ageostrophic velocity (in cm/s) for the month of February of model year 20 in the Gulf Stream extension region (red box in Figure 11), showing the background Ekman drift and anticyclonic flow in both the Warm Core Ring (WR) and Cold Core Ring (CR).

**Figure 13.** SSH power spectra in the energetic Gulf Stream extension region (red box in Figure 11) for the gridded <sup>1</sup>/<sub>4</sub>° AVISO (black line) and for the 1/50° HYCOM on its original grid (red), subsampled on the <sup>1</sup>/<sub>4</sub>° grid (green), 10-day average (blue), 150-km band pass (cyan), and combined 10-day average/150-km band pass (magenta).

*Figure 14.* Surface eddy kinetic energy (in cm<sup>2</sup>s<sup>-2</sup>) in the Gulf Stream region computed from SSHderived geostrophic velocities, a) the ¼ °AVISO, b) 1/50 ° HYCOM, c) 150-km band passed 1/50 ° HYCOM, and d) combined 10-day average/150-km band passed 1/50 ° HYCOM.

*Figure 15.* Vertical distribution of the modeled zonal velocity (cm/s) and eddy kinetic energy (cm<sup>2</sup>s<sup>-</sup><sup>2</sup>) along 55 °W for the 1/50°, 1/25°, and 1/12° simulations, respectively.

*Figure 16.* Vertical distribution of the observed zonal velocity (cm/s) and eddy kinetic energy (in cm<sup>2</sup>s<sup>-2</sup>) along 55 W based on current meter moorings and subsurface floats (from Richardson, 1985).

**Figure 17.** Horizontal distribution of eddy kinetic energy (in cm<sup>2</sup>s<sup>-2</sup>) at 700 meter from a) SOFAR float measurements (Richardson, 1993), and b-d) the 1/50°, 1/25°, and 1/12°HYCOM simulations, respectively (years 16-20).

*Figure 18.* Horizontal distribution of eddy kinetic energy (in  $cm^2s^{-2}$ ) at 1000 meter from a) Argo float measurements (Ollitrault and Colin de Verdiere, 2014), b) the 1/50° simulation, c) the 1/50° simulation with 30-day and 1° filters, d) the 1/25° simulation, and e) the 1/12° simulation.

*Figure 19.* SSH power spectra computed over the 20°x10° red box in Figure 11 using mirror (black) and tapered cosine windows of different size (none, 5%, 10%, 20% and 40%). Results based on 1-year average (year 20) of the 1/50° simulation.

**Figure 20.** SSH power spectra in the energetic Gulf Stream region (the 20°x10° box in Figure 11) computed from daily averaged model outputs of year 20 for 1/12°, 1/25°, and 1/50° simulations. The black lines are annual mean; red and blue lines are average over summer and winter, respectively. The green dash line corresponds to k-5 and the shaded area brackets the 70-250 km mesoscale range.

*Figure 21.* A snapshot of dimensionless surface relative vorticity ( $\zeta/f$  with  $f=10^{-4} s^{-1}$ ) in the Gulf Stream region in summer (August 31) and winter (March 1) of year 20 of the  $1/12^{\circ}$  simulation.

*Figure 22.* A snapshot of dimensionless surface relative vorticity ( $\zeta/f$  with  $f=10^{-4} s^{-1}$ ) in the Gulf Stream region in summer (August 31) and winter (March 1) of year 20 of the 1/50° simulation.

**Figure 23.** Power spectra in the energetic Gulf Stream region (red box in Figure 11) computed from daily averaged outputs of year 20 for the 1/50° configuration: a) SSH, b) total surface velocity, c) SSH-derived geostrophic velocity, and d) surface relative vorticity. Annual, summer, and winter mean power spectra are denoted in black, red, and blue, respectively.

*Figure 24.* Power spectra in a less energetic northeast Atlantic region (20-30 N, 20-40 W, see Figure 25) computed from daily averaged outputs of year 20 for the 1/50° configuration: a) SSH, b) total surface velocity, c) SSH-derived geostrophic velocity, and d) surface relative vorticity. Annual, summer, and winter mean power spectra are denoted in black, red, and blue, respectively.

*Figure 25.* Sea-surface height power spectra slopes (in the 70-250 km mesoscale range) for  $10x10^{\circ}$  boxes, calculated from on daily mean outputs for model year 20 of the  $1/50^{\circ}$  configuration.

**Figure 26.** Sea-surface height power spectra for the 10x10° boxes shown in Figure 25, calculated from daily means (solid lines) and hourly snapshots (dashed lines) for the month of December of year 20 of the 1/50° simulation. The captions in each panel indicate the western-most longitude of the box and the corresponding spectral slopes in the 70-250 mesoscale range (daily and hourly).



Figure 1. Model domain and bathymetry (in kilometers).



*Figure 2.* Time evolution of the domain-averaged kinetic energy (in  $cm^2s^{-2}$ ) for the three numerical experiments (1/12°, 1/25°, and 1/50°, respectively). The thin and thick lines denote monthly and annual averages, respectively.



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**Figure 4.** Kinetic energy (cm<sup>2</sup>s<sup>-2</sup>) of time mean surface geostrophic current based on a) the AVISO climatology CNES-CLS13, and b-d) the 1/50°, 1/25°, and 1/12°HYCOM simulations, respectively (years 16-20).



*Figure 5. a) Topex-Poseidon tracks (#932523A in red) superimposed on the mean SSH (in cm) from Niiler et al. (2203), b) observed mean dynamic topography (in cm) along track #932523A derived from 1) the in-situ bathythermographic data, 2) the AVISO climatology CNES-CLS13 and CNES-CLS09, and 3) the 1/50°, 1/25°, and 1/12° HYCOM simulations, respectively (years 16-20).* 



**Figure 6.** a) Mean velocity section as measured by the Oleander (1993-2012) with shipboard ACDP (55 m depth). The horizontal bar corresponding to 1 m/s and 0.5 m/s for the variance ellipse (from Rossby et al., 2014); and b-d) mean velocity for the 1/50°, 1/25°, and 1/12° HYCOM simulations, respectively (years 16-20). The depth contours range from 1000 to 5000 meters (grey shading).



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**Figure 13.** SSH power spectra in the energetic Gulf Stream extension region (red box in Figure 11) for the gridded <sup>1</sup>/<sub>4</sub> ° AVISO (black line) and for the 1/50 ° HYCOM on its original grid (red), subsampled on the <sup>1</sup>/<sub>4</sub> ° grid (green), 10-day average (blue), 150-km band pass (cyan), and combined 10-day average/150-km band pass (magenta).



**Figure 14.** Surface eddy kinetic energy (in cm<sup>2</sup>s<sup>-2</sup>) in the Gulf Stream region computed from SSHderived geostrophic velocities, a) the ¼ °AVISO, b) 1/50 ° HYCOM, c) 150-km band passed 1/50 ° HYCOM, and d) combined 10-day average/150-km band passed 1/50 ° HYCOM.



*Figure 15.* Vertical distribution of the modeled zonal velocity (cm/s) and eddy kinetic energy (cm<sup>2</sup>s<sup>-</sup><sup>2</sup>) along 55 °W for the 1/50 °, 1/25 °, and 1/12 ° simulations, respectively.



**Figure 16.** Vertical distribution of the observed zonal velocity (cm/s) and eddy kinetic energy (in cm<sup>2</sup>s<sup>-2</sup>) along 55 °W based on current meter moorings and subsurface floats (from Richardson, 1985).



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**Figure 19.** SSH power spectra computed over the 20°x10° red box in Figure 11 using mirror (black) and tapered cosine windows of different size (none, 5%, 10%, 20% and 40%). Results based on 1-year average (year 20) of the 1/50° simulation.



**Figure 20.** SSH power spectra in the energetic Gulf Stream region (the 20°x10° box in Figure 11) computed from daily averaged model outputs of year 20 for 1/12°, 1/25°, and 1/50° simulations. The black lines are annual mean; red and blue lines are average over summer and winter, respectively. The green dash line corresponds to k-5 and the shaded area brackets the 70-250 km mesoscale range.



*Figure 21.* A snapshot of dimensionless surface relative vorticity ( $\zeta/f$  with  $f=10^{-4} \text{ s}^{-1}$ ) in the Gulf Stream region in summer (August 31) and winter (March 1) of year 20 of the 1/12 ° simulation.



*Figure 22.* A snapshot of dimensionless surface relative vorticity ( $\zeta/f$  with  $f=10^{-4} \text{ s}^{-1}$ ) in the Gulf Stream region in summer (August 31) and winter (March 1) of year 20 of the 1/50° simulation.



**Figure 23.** Power spectra in the energetic Gulf Stream region (red box in Figure 11) computed from daily averaged outputs of year 20 for the 1/50° configuration: a) SSH, b) total surface velocity, c) SSH-derived geostrophic velocity, and d) surface relative vorticity. Annual, summer, and winter mean power spectra are denoted in black, red, and blue, respectively.



*Figure 24.* Power spectra in a less energetic northeast Atlantic region (20-30 %, 20-40 %, see Figure 25) computed from daily averaged outputs of year 20 for the 1/50° configuration: a) SSH, b) total surface velocity, c) SSH-derived geostrophic velocity, and d) surface relative vorticity. Annual, summer, and winter mean power spectra are denoted in black, red, and blue, respectively.



*Figure 25.* Sea-surface height power spectra slopes (in the 70-250 km mesoscale range) for  $10x10^{\circ}$  boxes, calculated from on daily mean outputs for model year 20 of the  $1/50^{\circ}$  configuration.



**Figure 26.** Sea-surface height power spectra for the 10x10° boxes shown in Figure 25, calculated from daily means (solid lines) and hourly snapshots (dashed lines) for the month of December of year 20 of the 1/50° simulation. The captions in each panel indicate the western-most longitude of the box and the corresponding spectral slopes in the 70-250 mesoscale range (daily and hourly).